# AN EARLY-STAGE APPROACH TO OPTIMISE THE SYNTHESIS, DESIGN AND OPERATION OF A MARINE ENERGY SYSTEM FOR LIQUEFIED NATURAL GAS CARRIERS 

Crístofer Hood Marques


#### Abstract

Tese de Doutorado apresentada ao Programa de Pós-graduação em Engenharia Oceânica, COPPE, da Universidade Federal do Rio de Janeiro, como parte dos requisitos necessários à obtenção do título de Doutor em Engenharia Oceânica.


Orientadores: Carlos Rodrigues Pereira
Belchior
Jean David Job Emmanuel
Marie Caprace

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TESE SUBMETIDA AO CORPO DOCENTE DO INSTITUTO ALBERTO LUIZ COIMBRA DE PÓS-GRADUAÇÃO E PESQUISA DE ENGENHARIA (COPPE) DA UNIVERSIDADE FEDERAL DO RIO DE JANEIRO COMO PARTE DOS REQUISITOS NECESSÁRIOS PARA A OBTENÇÃO DO GRAU DE DOUTOR EM CIÊNCIAS EM ENGENHARIA OCEÂNICA.

Examinada por:


Prof. Antonio Carlos Fernandes, Ph.D.

## Marques, Crístofer Hood

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Resumo da Tese apresentada à COPPE/UFRJ como parte dos requisitos necessários para a obtenção do grau de Doutor em Ciências (D.Sc.)

# UMA ABORDAGEM INICIAL PARA OTIMIZAR A SÍNTESE, PROJETO E OPERAÇÃO DE UM SISTEMA DE ENERGIA MARÍTIMO PARA NAVIOS TRANSPORTADORES DE GÁS NATURAL LIQUEFEITO 

Crístofer Hood Marques

Fevereiro/2018

Orientadores: Carlos Rodrigues Pereira Belchior<br>Jean David Job Emmanuel Marie Caprace

Programa: Engenharia Oceânica

Uma vez que as decisões de maior impacto são feitas nos primeiros estágios do projeto do navio, o desenvolvimento de ferramentas de projeto para disponibilizar mais informações mais cedo é desejável. Além disso, ainda há margem para melhorias na otimização da seleção do sistema de energia, considerando uma abordagem integrada. Portanto, o presente trabalho visa proporcionar uma abordagem preliminar e abrangente para a otimização de projeto, síntese e operação, considerando aspectos econômicos e técnicos, bem como o estado do mar ao longo da rota. Para evitar hélices que possam apresentar problemas de resistência, cavitação e vibração, são usadas restrições. Vários hélices, dezesseis motores e quatro perfis operacionais são avaliados. Um algoritmo de otimização do tipo evolução diferencial, cuja função objetivo a ser maximizada é o valor presente líquido, é aplicado. O estudo de caso foi projetado usando um transportador de gás natural liquefeito de $175,000 \mathrm{~m}^{3}$ que navega entre Lake Charles (EUA) e Tokyo Bay (Japão), através do Canal do Panamá. Todas as combinações adequadas para 15,023 hélices são encontradas. A abordagem mostra um ganho de $22 \%$ entre o pior indivíduo da população inicial e o pior indivíduo da população final. A potência no freio necessária é aproximadamente $22 \%$ maior para mar agitado do que para água parada. Uma diferença de mais de $120 \%$ foi encontrada comparando combinações variadas de cenas econômicas e perfis de combustível. A abordagem mostra um ganho significativo e destaca o valor de explorar uma ampla gama de configurações de sistemas de energia de forma integrada, considerando a condição climática.

Abstract of Thesis presented to COPPE/UFRJ as a partial fulfillment of the requirements for the degree of Doctor of Science (D.Sc.)

# AN EARLY-STAGE APPROACH TO OPTIMISE THE SYNTHESIS, DESIGN AND OPERATION OF A MARINE ENERGY SYSTEM FOR LIQUEFIED NATURAL GAS CARRIERS 

Crístofer Hood Marques

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Advisors: Carlos Rodrigues Pereira Belchior<br>Jean David Job Emmanuel Marie Caprace<br>Department: Ocean Engineering

Since decisions of the greatest impact are made in early stages of ship design, developing design tools to make more information available sooner is desirable. Moreover, there is still room for improvements on the optimisation of energy system selection considering an integrated approach. Therefore, the present work aims to provide a comprehensive early-stage approach to perform the optimisation of design, synthesis and operation, considering economic and technical aspects as well as route weather. Constraints are used to avoid propellers that could present issues concerning strength, cavitation and vibration. Various propellers, sixteen engines and four operational profiles are assessed. A differential evolution optimisation algorithm whose objective function to be maximised is the net present value is applied. The case study is designed using a liquefied natural gas carrier of 175,000 $\mathrm{m}^{3}$ sailing between Lake Charles (USA) and Tokyo Bay (Japan), via Panama Canal. All suitable matchings for 15,023 propellers are found. The approach shows a gain of $22 \%$ between the worst individual of the initial population and the worst individual of the final population. The required brake power is approximately $22 \%$ higher for rough weather than for still water. A difference of over $120 \%$ was found by comparing varied matchings of economic scenes and fuel profiles. The approach shows a significant gain and highlights the value of exploring a broad range of energy system configurations in an integrated manner, considering the weather condition.

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## List of Abbreviations

| 0-DEM | Zero-dimensional engine model, p. 8 |
| :---: | :---: |
| BN | Beaufort number [-], p. 41 |
| BOG | Boil-off gas, p. 1 |
| BOR | Boil-off rate [\%], p. 1 |
| CAPEX | Capital expenditure [US\$], p. 9 |
| CEAS-ERD | Computerised Engine Application System - Engine Room Dimensioning, p. 15 |
| CFD | Computational fluid dynamics, p. 8 |
| COGES | Combined gas turbine electric and steam system, p. 5 |
| CTU | Collecting tank unit, p. 17 |
| DFDD | Dual-fuel direct drive, p. 12 |
| DFDE | Dual-fuel Diesel electric, p. 12 |
| DOP | Dynamic optimisation problem, p. 81 |
| ECA | Emission control area, p. 16 |
| EGR | Exhaust gas recirculation, p. 2 |
| EM | Engine margin [-], p. 46 |
| FP | Fuel profile, p. 57 |
| FW | Freshwater, p. 17 |
| GCU | Gas combustion unit, p. 11 |
| HC | Hydrocarbons, p. 16 |
| HFO | Heavy fuel oil, p. 11 |

HP High pressure, p. 12
IMO International Maritime Organisation, p. 16
ISO International Organisation for Standardisation, p. 22
LCB Longitudinal centre of buoyancy [\%], p. 54
LNGC Liquefied natural gas carrier, p. 1
LNG Liquefied natural gas, p. 1
LP Low pressure, p. 12
MCR Maximum continuous rating, p. 46
MDO Marine diesel oil, p. 11
MEP Mean effective pressure [Pa], p. 14
MF Exhaust gas mass flow $[\mathrm{kg} / \mathrm{s}]$, p. 24
MGO Marine gas oil, p. 11
MVEM Mean value engine model, p. 5
NMCR Nominal maximum continuous rating, p. 15
NPV Net present value [US\$], p. 5
OPEX Operational expenditure [US\$], p. 2
PM Particulate materials, p. 2
PPI Producer price index [-], p. 48
PT Power turbine, p. 21
RT Route-track, p. 56
SCR Selective catalytic reduction, p. 2
SDO Synthesis, design and operation, p. 62
SFC Specific fuel consumption, p. 50
SFOC Specific fuel oil consumption $[\mathrm{g} / \mathrm{kWh}]$, p. 24
SGC Specific gas consumption [g/kWh], p. 24

SMCR Specified maximum continuous rating, p. 14
SMF Specific exhaust gas mass flow $[\mathrm{kg} / \mathrm{kWh}]$, p. 24
SM Service margin [-], p. 42
SPOC Specific pilot oil consumption $[\mathrm{g} / \mathrm{kWh}]$, p. 24
ST Specific temperature [K/MW], p. 24
ST Steam turbine, p. 21
SW Seawater, p. 18
TFEM Transfer function engine model, p. 8
WCU Water cleaning unit, p. 18
WHRS Waste heat recovery system, p. 3
WTU Water treatment unit, p. 17

## List of Symbols

| $1+k_{1}$ | Form factor of the hull [-], p. 41 |
| :---: | :---: |
| $A_{E} / A_{O}$ | Blade-area ratio [-], p. 43 |
| $A_{p}$ | Projected area of the propeller [ $\mathrm{m}^{2}$ ], p. 44 |
| $A_{B T}$ | Transverse bulb area $\left[\mathrm{m}^{2}\right]$, p. 54 |
| B | Moulded breadth [m], p. 45 |
| CAPEX ${ }_{m}$ | Capital expenditure on machinery [US\$], p. 48 |
| $C A P E X_{r p}$ | Capital expenditure on the re-liquefaction plant [US\$], p. 48 |
| $C I F_{L N G}$ | Cost-insurance-freight price of liquefied natural gas [US\$/kg], p. 51 |
| $C R$ | Crossover factor [-], p. 52 |
| $C_{M}$ | Midship section coefficient [-], p. 54 |
| $C_{U}$ | Speed reduction coefficient [-], p. 41 |
| $C_{\beta}$ | Direction reduction coefficient [-], p. 39 |
| $C_{m}$ | Maintenance cost [US\$], p. 49 |
| $C_{n}$ | Coefficient dependent on vibration order and ship type [-], p. 45 |
| $C_{L N G}$ | Purchase cost of the LNG cargo [US\$], p. 49 |
| $C_{W P}$ | Water-plane area coefficient [-], p. 54 |
| $C_{f, G}$ | Total gaseous fuel cost [US\$], p. 50 |
| $C_{f, O}$ | Total fuel oil cost [US\$], p. 50 |
| $C_{f, P O}$ | Total pilot oil cost [US\$], p. 50 |


| $C_{f, o t h}$ | Fuel cost related to other consumers on-board, p. 49 |
| :---: | :---: |
| $C_{f, p L}$ | Total liquid fuel cost [US\$], p. 50 |
| $C_{f, p r o}$ | Fuel cost related to propulsion [US\$], p. 49 |
| $C_{f, r e l}$ | Fuel cost related to boil-off gas re-liquefaction [US\$], p. 49 |
| $C_{\text {form }}$ | Ship form coefficient [-], p. 41 |
| $C_{\text {jou }}$ | Journey cost [US\$], p. 49 |
| $C_{m, E}$ | Engine maintenance cost [US\$], p. 51 |
| $C_{\text {stern }}$ | Stern shape parameter [-], p. 54 |
| D | Propeller diameter [m], p. 43, 44 |
| $D_{m}$ | Moulded depth [m], p. 45 |
| $E_{I D}$ | Engine identification [-], p. 59 |
| F | Mutation factor [-], p. 52 |
| $F O B_{L N G}$ | Free-on-board price of liquefied natural gas [US\$], p. 49 |
| $F P_{I D}$ | Fuel profile identification [-], p. 59 |
| Fy | Annual net cash flow [US\$/year], p. 51 |
| $J$ | Advance ratio [-], p. 43 |
| $K_{Q}$ | Torque coefficient [-], p. 43 |
| $K_{T}$ | Thrust coefficient [-], p. 43 |
| $L$ | Length on waterline [m], p. 54 |
| $L H V_{g}$ | Standard lower heating value for gaseous fuel [J/kg], p. 54 |
| LHV ${ }_{l}$ | Standard lower heating value for liquid fuel [ $\mathrm{J} / \mathrm{kg}$ ], p. 54 |
| $L H V_{B O G}$ | Lower heating value of boil-off gas [J/kg], p. 54 |
| $L H V_{H F O}$ | Lower heating value of heavy fuel oil [J/kg], p. 55 |
| $L H V_{M G O}$ | Lower heating value of marine gas oil [ $\mathrm{J} / \mathrm{kg}]$, p. 55 |
| $L_{s}$ | Shaft length [m], p. 49 |

$L_{p p} \quad$ Length between perpendiculars [m], p. 45
$L x \quad$ Points defining an engine envelop, where $x$ may be $1,2,3$ or 4, p. 14
$P / D \quad$ Pitch ratio [-], p. 43
$P_{B} \quad$ Brake power [W], p. 24
$P_{O} \quad$ Open water power [W], p. 43
$P_{S} \quad$ Power delivered by each blade [W], p. 44
$P_{B, r w} \quad$ Brake power in rough weather [W], p. 68
$P_{B, s w} \quad$ Brake power in still water [W], p. 69
$P_{B c, x} \quad$ Brake power per cylinder, where $x$ may be L1, L2, L3 or L4 [W/cyl], p. 23
$P_{M C R} \quad$ Brake power at the maximum continuous rating point [W], p. 46
$P_{N M C R} \quad$ Brake power at the nominal maximum continuous rating point [W], p. 49
$P_{S M C R} \quad$ Brake power at the specified maximum continuous rating point [W], p. 46
$P_{\text {com }} \quad$ Electric power required by the BOG compression system [W], p. 50
$P_{i, j+1} \quad$ One offspring member, p. 52
$P_{i, j} \quad i^{\text {th }}$ individual of the $j^{\text {th }}$ generation of the population $\Pi$, p. 52
$P_{\text {oth }} \quad$ Electric power required by other consumers [W], p. 50
$Q \quad$ Torque [Nm], p. 43
$R \quad$ Random number between 0 and $1[-]$, p. 52
$R_{A} \quad$ Model-ship correlation resistance [ N ], p. 41
$R_{B} \quad$ Additional pressure resistance of bulbous bow near the water surface [N], p. 41
$R_{F} \quad$ Frictional resistance [N], p. 41

| $R_{W}$ | Wave resistance [ N ], p. 41 |
| :---: | :---: |
| $R_{n}$ | Reynolds number, p. 43 |
| $R_{A P P}$ | Appendage resistance [ N ], p. 41 |
| $R_{T, r w}$ | Total propulsion resistance in rough weather [N], p. 65 |
| $R_{T, s e r}$ | Total resistance in service [ N$]$, p. 42 |
| $R_{T, s w}$ | Total propulsion resistance in still water [ N$]$, p. 39 |
| $R_{T, t r i}$ | Trial total resistance [ N ], p. 42 |
| $R_{T R}$ | Additional pressure resistance due to transom immersion [ N ], p. 41 |
| $S$ | Route-track length [m], p. 56 |
| $S F C_{G E}$ | Specific fuel consumption of the generation engine $[\mathrm{g} / \mathrm{kWh}]$, p . 50 |
| $S F O C_{G E}$ | Specific fuel oil consumption of generation engines $[\mathrm{g} / \mathrm{kWh}], \mathrm{p}$. |
| $S F O C_{H F O}$ | Specific heavy fuel oil consumption [g/kWh], p. 56 |
| $S G C_{B O G}$ | Specific boil-off gas consumption [g/kWh], p. 56 |
| $S G C_{G E}$ | Specific gas consumption of generation engines [g/kWh], p. 54 |
| $S P O C_{G E}$ | Specific pilot oil consumption of generation engines $[\mathrm{g} / \mathrm{kWh}]$, p. 54 |
| $S P O C_{H F O}$ | Specific pilot heavy fuel oil consumption [g/kWh], p. 56 |
| $S P_{B O G}$ | Power required to re-liquefy a mass flow unit of boil-off gas [Ws/kg], p. 50 |
| $S_{C}$ | Maximum allowable stress of the propeller material [Pa], p. 44 |
| $T$ | Temperature [K], p. 24 |
| $T_{m}$ | Draught moulded [m], p. 54 |
| Th | Thrust [ N ], p. 42 |
| $V_{S}$ | Cylinder swept volume [m³, p. 24 |

$V_{h} \quad$ Heel volume $\left[\mathrm{m}^{3}\right]$, p. 49
$V_{B O G} \quad$ Total volume of liquefied natural gas becoming boil-off gas, including naturally and forced generated amounts [ $\mathrm{m}^{3}$ ], p. 49
$V_{L N G} \quad$ Volume of liquefied natural gas in the tanks $\left[\mathrm{m}^{3}\right]$, p. 50
$V_{\text {rel }} \quad$ Volume of liquefied natural gas coming from the re-liquefaction plant [ $\mathrm{m}^{3}$ ], p. 49
$V d_{L N G} \quad$ Volume of liquefied natural gas delivered at unloading terminal [m³, p. 51
$V p_{L N G} \quad$ Cargo volume of liquefied natural gas purchased at loading terminal $\left[\mathrm{m}^{3}\right]$, p. 49
$V t_{L N G} \quad$ Ship's total cargo capacity in volume $\left[\mathrm{m}^{3}\right]$, p. 49
$W R C_{m} \quad$ Machinery weight-related cost [US\$ $/ \mathrm{kg}$ ], p. 48
$W R C_{r p} \quad$ Weight-related cost of the re-liquefaction plant [US\$ $/ \mathrm{kg}$ ], p. 48
$W_{m} \quad$ Machinery weight $[\mathrm{kg}]$, p. 48
$W_{p} \quad$ Propeller weight $[\mathrm{kg}]$, p. 49
$W_{s} \quad$ Shaft weight $[\mathrm{kg}]$, p. 49
$W_{r p} \quad$ Re-liquefaction plant weight $[\mathrm{kg}]$, p. 48
$Z \quad$ Number of blades, p. 43
$Z_{c} \quad$ Number of cylinders of an engine, p. 23
$Z_{p} \quad$ Number of propellers, p. 42
$\Delta t_{r n d} \quad$ Period to accomplish a round trip $[\mathrm{s}], \mathrm{p} .63$
$\Delta_{V} \quad$ Displacement including the virtual added mass of water $[\mathrm{kg}]$, p. 45
$\Pi \quad$ Population, p. 52
$\alpha, \beta, \gamma \quad$ Randomly chosen members of the population $\Pi$, p. 52
$\delta t \quad$ Duration of a certain condition [s], p. 50
$\delta_{1}, \delta_{2} \quad$ Functions related to crossover, p. 52

| $\dot{m}_{\text {BOGc }}$ | Total mass flow of boil-off gas consumed, p. 50 |
| :---: | :---: |
| $\dot{m}_{B O G g}$ | Mass flow of boil-off gas naturally generated [kg/s], p. 50 |
| $\dot{m}_{B O G r}$ | Mass flow of boil-off gas to be re-liquefied [kg/s], p. 50 |
| $\eta_{G}$ | Generator efficiency [\%], p. 50 |
| $\eta_{O}$ | Open water efficiency [\%], p. 43 |
| $\eta_{R}$ | Relative rotative efficiency [\%], p. 42 |
| $\eta_{S}$ | Shaft efficiency [\%], p. 46 |
| $\eta_{E, a v g}$ | Average engine efficiency [\%], p. 63 |
| $\eta_{G B}$ | Gearbox efficiency [\%], p. 46 |
| $\eta_{O, a v g}$ | Average open water efficiency [\%], p. 63 |
| $\mu$ | Mean, p. 27 |
| $\nabla$ | Moulded displacement volume [m ${ }^{3}$ ], p. 54 |
| $\rho$ | Density of the water $\left[\mathrm{kg} / \mathrm{m}^{3}\right]$, p. 43 |
| $\rho_{L N G}$ | Density of the liquefied natural gas $\left[\mathrm{kg} / \mathrm{m}^{3}\right]$, p. 49 |
| $\sigma$ | Standard deviation, p. 27 |
| $\sigma_{0.7 R}$ | Mean cavitation number [-], p. 44 |
| $\tau_{c 0.7 R}$ | Thrust loading coefficient [-], p. 44 |
| $\theta_{l}$ | Encounter angle for laden trip [], p. 56 |
| $c_{m}$ | Maintenance unit cost [US\$/Ws], p. 59 |
| $c_{\text {HFO }}$ | Unit cost of heavy fuel oil [US\$/kg], p. 59 |
| $c_{M G O}$ | Unit cost of marine gas oil [US $\$ / \mathrm{kg}$ ], p. 59 |
| $c_{l f}$ | Liquid fuel unit cost [US $\$ / \mathrm{kg}$ ], p. 50 |
| $f$ | Excitation frequency due to the propeller [Hz], p. 46 |
| $f_{\text {ins }}$ | Installation cost factor [-], p. 49 |
| $h_{B}$ | Centre of bulb area above keel line [m], p. 54 |

$h_{s} \quad$ Centre of propeller shaft above keel line [m], p. 55
$m_{L N G} \quad$ Mass of liquefied natural gas delivered per round trip [kg], p. 63
$n_{r n d} \quad$ Number of round trips a year, p. 51
Engine shaft speed [rev/s], p. 23
Number of generations [-], p. 60
Number of individuals in the population $\Pi[-]$, p. 60
Integer related to the harmonics [-], p. 46
Engine rated speed $[\mathrm{rev} / \mathrm{s}]$, p. 16
Period of economic analysis [year], p. 51 [rev/s], p. 46 point [rev/s], p. 49

Number of route-tracks in ballast, p. 49
Number of route-tracks in laden, p. 51 point [rev/s], p. 46

Shaft speed in rough weather $[\mathrm{rev} / \mathrm{s}]$, p. 68
Shaft speed in still water $[\mathrm{rev} / \mathrm{s}]$, p. 68
Water vapour pressure [Pa], p. 44
Static pressure at the shaft centre line [Pa], p. 44 [rev/cycle], p. 24

Discount rate [\%], p. 51
Service margin component due to displacement [-], p. 42
Service margin component due to fouling [-], p. 42

Engine shaft speed at the maximum continuous rating point

Engine shaft speed at the nominal maximum continuous rating

Engine shaft speed at the specified maximum continuous rating

Revolutions of crankshaft per complete working cycle

| $s m_{h}$ | Service margin component due to the hull form [-], p. 42 |
| :---: | :---: |
| $s m_{w}$ | Service margin component due to weather [-], p. 42 |
| $s m_{w d}$ | Service margin component due to water depth [-], p. 42 |
| $t$ | Thrust deduction factor [-], p. 42 |
| $t_{0.75 R}$ | Blade thickness at $75 \%$ of the propeller radius [m], p. 44 |
| $v_{A}$ | Advance velocity of the propeller [m/s], p. 42 |
| $v_{10}$ | Wind speed at a height of 10 m above sea level [m/s], p. 41 |
| $v_{r w, h b}$ | Higher level of service speed in ballast [m/s], p. 59 |
| $v_{r w, h l}$ | Higher level of service speed in laden [m/s], p. 59 |
| $v_{r w, i b}$ | Intermediary level of service speed in ballast [m/s], p. 59 |
| $v_{r u, i l}$ | Intermediary level of service speed in laden [m/s], p. 59 |
| $v_{r w, l b}$ | Lower level of service speed in ballast [m/s], p. 59 |
| $v_{r w, l l}$ | Lower level of service speed in laden [m/s], p. 59 |
| $v_{r w}$ | Service speed in rough weather [m/s], p. 39 |
| $v_{s w}$ | Service speed in still water [m/s], p. 39 |
| $v_{\text {tip }}$ | Blade tip peripheral velocity [m/s], p. 45 |
| $w$ | Wake factor [-], p. 42 |

## Chapter 1

## Introduction

Next, it is presented a background about liquefied natural gas carriers, their energy system and propulsion design. The state of the art about simulation and optimisation of the ship energy system is presented subsequently. At the end of this chapter, the doctoral dissertation proposal is addressed.

### 1.1 Background

Liquefied natural gas carriers (LNGCs) are specialised ships designed to transport liquefied natural gas (LNG). They are fitted with insulated double-hulled tanks with basically two types of geometry, such as shown in Fig. 1.1. The tanks are designed to contain the cargo slightly above atmospheric pressure at a cryogenic temperature without any means of external refrigeration. Typically, the storage tanks operate at $0.3 \mathrm{bar}_{g}{ }^{1}$ with a design pressure of $0.7 \mathrm{bar}_{g}$ and a negative temperature around $-169{ }^{\circ} \mathrm{C}$, such that the LNG density lies between 430 and $470 \mathrm{~kg} / \mathrm{m}^{3}$, depending on its composition and state. The composition is predominantly methane $\left(\mathrm{CH}_{4}\right)$ and smaller fractions of ethane $\left(\mathrm{C}_{2} \mathrm{H}_{6}\right)$, propane $\left(\mathrm{C}_{3} \mathrm{H}_{8}\right)$, butane $\left(\mathrm{C}_{4} \mathrm{H}_{10}\right)$ and nitrogen $\left(\mathrm{N}_{2}\right)$.

Despite the high level of insulation of the cargo tanks, some vaporisation occurs because it is impossible to avoid the heat transfer from the surroundings to the cargo. This evaporated LNG is called boil-off gas (BOG) and its evaporation rate, which is called boil-off rate (BOR), is generally about 0.10 to $0.15 \%$ in volume per day, depending on the thermal insulation system [1]. In this sense, a detailed dynamic BOG model, which accounts for the variation of mass flow, composition and thermodynamic properties, was developed in [2]. Since vaporisation induces a pressure increase in the tank, a certain amount of the vapour phase should be taken out of the tank to avoid dangerous overpressure. Usually, this outlet gas flow is used

[^0]as fuel by the marine energy system of the ship to reduce its main fuel consumption [3].


Figure 1.1: LNGCs with different cargo tank geometries.
For many years steam propulsion plants were practically an exclusive option for LNGCs due to its capability to burn the unavoidable BOG directly in the power boiler. However, as environmental, economic and technical expectations have increased, the drawbacks of the steam turbine power plant have made it a less attractive option. Among these drawbacks is the comparatively low efficiency of the plant, its high fuel consumption, high exhaust emissions and large engine room space requirement. On the other hand, advances in the design of dual-fuel Diesel engines, shipboard BOG re-liquefaction plants, and marine gas turbines, provide meaningful alternatives to the traditional steam power plant. Moreover, propulsion systems based on slow speed two-stroke Diesel engines driving fixed pitch propellers with the inboard re-liquefaction system have been successfully used in large LNGCs.

However, when conventional fuel prices are higher than LNG price, the operational expenditure (OPEX) of propulsion systems that are unable to use BOG as fuel is increased [1]. Moreover, conventional fuels are not as clean as the BOG, once natural gas is considered environmentally friendly for various reasons [4]. Thus, an option to overcome these drawbacks is to apply dual-fuel Diesel engines, which are compression ignition ones capable to work in two operational modes: Diesel mode and gas mode [5].

Owing to environmental concerns, controls on exhaust gas emissions continue to tighten regionally and internationally dictating further responses from engine designers. Carbon dioxide $\left(\mathrm{CO}_{2}\right)$, nitrogen oxides $\left(\mathrm{NO}_{x}\right)$, sulphur oxides $\left(\mathrm{SO}_{x}\right)$ and particulate materials (PM) are the gaseous emissions of most concern. Thereby, in-engine measures to decrease these emissions, including common rail fuel systems, emulsified fuel, direct water injection and charge air humidification, have been studied. In addition, exhaust gas after-treatment, such as selective catalytic reduction (SCR) and exhaust gas recirculation (EGR) systems, as well as gas scrubbers, also have been developed for this purpose.

Regarding the reduction of $\mathrm{CO}_{2}$ emission, the solutions are mainly burning
alternative fuels, as BOG for instance, and decreasing the fuel consumption. The latter is achieved by means of the increase of the ship energy efficiency. Measures that positively affect it include the improved hull and ship structure designs, which result in decreased ship resistance, as well as more efficient thrusters designs that can increase the ship propulsive efficiency. Further, more efficient propulsion types and the exploitation of the rejected energy as much as possible have been pursued. In this sense, waste heat recovery systems (WHRSs) have emerged [5].

Since the prime mover is usually operated until the end of the ship's lifetime, its selection is one of the major steps in merchant shipbuilding projects. Although a complete criteria list for choosing main machinery is given in [6] and many considerations are presented in [7, BULUT et al. 8] defined six major selection criteria. Based on interviews with a group of technical experts and managers of selected shipping companies, the author highlighted: power, acquisition cost, fuel consumption, maintenance, the majority in existing merchant fleet and damage history of the model.

Power is on the top of the list because the engine needs to be capable to provide enough power to satisfy the ship's operational profile. Acquisition cost is considered one of the major indicators of the financial feasibility of a project because it represents about $10 \%$ of the total cost of a new building project. Another significant indicator of financial feasibility is fuel consumption. Maintenance attributes can though divide into two considerations: firstly, how easy it can be performed and secondly, how much it costs.

Differently, majority in existing merchant fleet, or common practice, is an important aspect for other reasons. If a specific model and brand of Diesel engine are frequently preferred, this may denote its superiority in overall circumstances. A similar indicator is the damage history of the model, or reliability, which illustrates its structural and mechanical hardness in the practical life. These two latter criteria illustrate why the design of a new machinery system is typically done by considering a traditional concept as a base [9].

For ships navigating across large oceans, considerations about the weather conditions are essential for safe and efficient operations. The environment exposes the ship to loads from wind, waves, and currents changing the operating point of the ship's energy system [10]. To ensure safe passage, arrival on time, minimized operational costs and minimal environmental impact it is important that the weather expected to be found throughout the route is taken into account since the early-stage project. Thus, the integrated nature of a ship energy system makes the collaboration among multiple engineering disciplines to be required in the design process.

Furthermore, one of the challenges of ship design is that the decisions of the greatest impact are made in early stages of design when the least information
and greatest uncertainty are present [11]. Hence, developing ship design tools to make more information available sooner and pushing decision points for later is quite advisable. In this sense, simulations of the overall ship energy system and optimisation studies are of great interest.

### 1.2 State of the art

Studies about ship energy system simulation and optimisation were briefly discussed below in order to present the state of the art overview.

BENVENUTO et al. [12] presented a computer simulation model able to predict the dynamic behaviour of a whole marine propulsion system and to evaluate the influence of its three main elements: ship, propeller and prime mover. The developed procedure was able to represent the system operating both in steady-state and in transient conditions (manoeuvring). The adoption of a fixed pitch versus a controllable pitch propeller and various choices relative to the plant control system were assessed.

KYRTATOS et al. [13] carried out a propulsion plant simulation of a container ship to assess the engine performance in different operating conditions. This paper considered the application of a detailed mathematical model for the prediction of the transient response of a large two-stroke marine Diesel engine. Load fluctuations caused by either change in the requested engine speed set point or by load changes were assumed to simulate severe weather conditions. The simulation module consisted of a Diesel engine model for performance prediction plus appended models for the shaft, propeller, and ship hull dynamics, as well as for the engine speed governor.

MICHALSKI [14] conceived an algorithmic method for preliminary selection of parameters of a ship propulsion system fitted with fixed pitch propeller and Diesel engine. The case study was about inland navigation, where hull resistance and service speed varies significantly, and the objective function was minimising the total fuel expenditure for a given voyage distance and time. Wageningen propellers of Ka series operating with 19A nozzles were considered, but the engine was taken simply as a constant figure of specific fuel consumption.

CHEN and SHIH [15] addressed a two-objective parametric optimisation problem regarding Wageningen B-screw series propeller design. The objective function was set by users who could freely weight the relative importance of the propeller's open water efficiency and vibration. Cavitation and strength constraints were considered and the vibration forces and moments were computed by a modified version of a program developed at the University of Michigan.

DIMOPOULOS et al. [16] performed a study focused on the optimisation of synthesis, design, and operation of a marine energy system for a cruise liner fitted with a combined gas turbine electric and steam system (COGES). Various configuration options, types of technologies and existence of components were incorporated. In addition, time-varying operational requirements were considered, resulting in a time-dependent operation optimisation problem. The complete optimisation problem was solved using a novel algorithm, inspired by evolutionary and social behaviour metaphors. A parametric analysis with respect to the fuel price demonstrated changes in the optimal synthesis of the system. The objective function of this optimisation was maximising the net present value (NPV). Similar works about LNGCs fitted with COGES, which also did not model either the propeller or the ship movement, are [17] and [18].

THEOTOKATOS [19] investigated the transient response of the overall ship propulsion plant for a merchant ship under various operating conditions. The two-stroke marine Diesel engine was approached by means of a mean value engine model (MVEM) and the propeller was modelled by the Wageningen B-screw series polynomials. In addition, the ship movement along its longitudinal axis was calculated using the differential equation of surge dynamics and the ship resistance was considered as a second order function of the velocity.

ALDOUS and SMITH [20] described a speed optimisation model for LNGCs considering ship geometric parameters, propeller characteristics, and engine specifications. The effect of various economic input parameters on the optimal speed for profit maximisation and cost minimisation were explored. A medium speed four-stroke dual-fuel Diesel engine with electric transmission and a conventional two-stroke engine with direct drive transmission were compared. The ship resistance was calculated using the Holtrop method and the Wageningen B-screw series polynomials were used to model propellers. Both engines were modelled by catalogue values.

THEOTOKATOS and TZELEPIS [21] carried out the mapping of performance and emission parameters for a merchant vessel propulsion system over the ship operating envelop. Thus, the system was simulated at various ship resistance conditions in the range from still water up to $55 \%$ added resistance. The two-stroke marine Diesel engine was approached by a MVEM and the Wageningen B-screw series polynomials were used to model the propeller. The ship resistance for still water was estimated by using the Holtrop method.

DIMOPOULOS et al. [22] presented the DNV COSSMOS modelling framework for integrated marine machinery systems. This is a tool based on mathematical descriptions of the physical and chemical process phenomena within machinery components and energy systems. It is capable to model, simulate and optimise
ship energy systems in the steady state and transient conditions. Two case studies were performed to illustrate the advantages of this: the thermo-economic design and operation optimisation of a combined cycle system for large bulk carriers, and the transient operation simulation of an electric marine propulsion system.

MAN [23] presented an overview about LNGCs fitted with slow speed dual-fuel Diesel engines of HP concept and the high-pressure gas supply system. Furthermore, ordinary and dual-fuel Diesel engines within various configurations were compared in order to show the most suitable propulsion solution for modern ships. Configurations with one and two engines driving directly fixed and controllable pitch propellers, with and without re-liquefaction system, were addressed. Three different sizes of LNGCs were studied and the measure of merit used for the comparison was NPV.

CICHOWICZ et al. [24] introduced a methodology of assessing the dynamic energy performance of a ship at a global level for any given period of time. All the major energy systems inboard were modelled and integrated into an overall energy model, which was subjected to a set of environmental conditions and operational requirements. In this manner, the energy flows inboard were presented as a function of time for four case studies. A MVEM was used for modelling the engine, the Wageningen B-screw series polynomials were used for modelling the propeller and the still water resistance was estimated by the Holtrop method.

LU et al. [25] developed an accurate and practical ship operational performance prediction model that can be used to select the optimal routes for minimum fuel consumption, taking into consideration average ship speed, encountering sea states and voyage time. This model was developed by modifying the Kwon added resistance modelling method for taking into account the ship's specific characteristics achieved from its operational data (ship's noon reports) and sea trial data. The Holtrop method was used to estimate the still water resistance of the ship. Besides, a time-dependent fuel consumption increase rate after ship dry-docking was identified.

YANG and YEH [26] investigated the thermodynamic and economic performance optimisation for an organic Rankine cycle system recovering the waste heat of exhaust gas from a large marine Diesel engine for a merchant ship. A number of working fluids was employed in the ORC system with and without pre-heater equipped to evaluate the system's maximal performances. Besides the optimal operating pressures, the optimal pre-heater effectiveness for each working fluid was obtained. The measures of merit used in this work were thermal efficiency and net power output index.

Table 1.1 summarises particularities found in the literature references to be considered or improved by the approach to be proposed. It is worth noticing that not all of these features are aimed to be dealt with herein. They serve as a guide to identify the current research gap in that field and elaborate the dissertation proposal.

Table 1.1: Features of the references to be considered or improved.

| Reference | To be considered | To be improved |
| :---: | :---: | :---: |
| [12] | + dynamic simulation | - engine as 2D table |
|  | + simplicity | - service speed as output |
| [13] | + dynamic simulation | - service speed disregarded |
|  | + various operating conditions <br> + two-stroke Diesel engine | - ship not modelled |
| [14] | + propeller optimisation | - Keller's cavitation criterion |
|  | + service speed optimisation | - fuel cost minimisation |
|  | + changeable operating conditions and hull resistance | - constant specific fuel consumption |
| [15] | + genetic algorithm | - Keller's cavitation criterion |
|  | + strength constraint | - efficiency maximisation |
|  | + vibration consideration | - only propeller study |
| [16] | + synthesis, design and operation optimisation | - propeller and hull disregarded |
|  | + particle swarm algorithm | - costs minimisation |
| [17, 18] | + synthesis, design and operation optimisation | - propeller and hull disregarded |
|  | + NPV maximisation | - weather disregarded |
|  | + particle swarm algorithm | - COGES system |
| [19] | + dynamic overall propulsion simulation | - optimisation disregarded |
|  | + two-stroke Diesel engine | - propulsion selection disregarded |
| [20] | + pitch ratio optimisation | - efficiency maximisation |
|  | + speed optimisation | - profit maximisation |
|  | + dual-fuel Diesel engine | - one operating condition |
| [21] | + overall propulsion simulation | - optimisation disregarded |
|  | + several operating conditions <br> + emissions estimation | - arbitrary service margins |
| [22] | + simulation and optimisation <br> + components model library | - DNV COSSMOS software |
| [23] | + dual-fuel two-stroke Diesel engine | - optimisation disregarded |
|  | + system with and without re-liquefaction <br> + emission fees | - arbitrary service margin |
| [24] | + systematic and scientific approach | - optimisation disregarded |
|  | + integrated overall energy model | - selection disregarded |
| [25] | + weather consideration | - minimising fuel consumption |
|  | + route optimisation | - system selection disregarded |
| [26] | $\begin{aligned} & +\quad \text { thermodynamics and } \\ & \text { economics } \\ & + \text { equipment cost evaluation } \end{aligned}$ | - propulsion disregarded |

### 1.2.1 Gap to be filled

None reference studying optimisation of energy system selection, considering engine, propeller and weather conditions within an integrated approach, has been found. The lack of studies about optimisation of Diesel engine selection might arise from the lack of engine models suitable for optimisation problems. According to SCHULTEN [27], five main sorts of engine models could be recognised: computational fluid dynamics (CFD) models, phenomenological multi-dimensional models, crank angle models, mean value models and transfer function models.

Within CFD engine models, which are the most complexes, the volume studied is divided into thousands of volumes or elements, and the basic conservation equations are solved for each volume. Being usually used only for processes occurring inside the cylinder and the ducts of admission and discharge, this modelling provides detailed information and requires powerful computers, besides high computational time. On the other hand, if the cylinder is divided into a smaller number of volumes (tens) and, additionally to the basic conservation equations, phenomenological equations are solved, a phenomenological multi-dimensional model is obtained. These both approaches are definitely not suitable for optimisation problems considering the overall energy system of a ship.

Crank angle models are also called zero-dimensional engine models (0-DEMs) because these models do not have a strict mathematical dependence on any of the dimensions. It consists in treating each one of the various engine elements as a control volume and solving the differential equations with a time step equivalent to one degree of the crankshaft rotation. Nevertheless, whether an engine model is inserted into a larger system, such as a propulsion system, the variations that occur for each crankshaft angle of rotation are generally not of primary interest. In this case, overall engine operating parameters are the focus and they can be obtained by using a MVEM. This model basically has the same origin of the 0-DEM, but as its time step is in the order of one crankshaft rotation, the variation of each parameter within the cylinder is replaced by a mean value. Some references about 0-DEMs are [13, 28, 30], whereas MVEMs were addressed in [19, 21, 24, 31, 33]. Besides those, a combination of MVEM and 0-DEM for a large marine four-stroke Diesel engine was presented in 34].

When there is no interest in the engine's internal processes, the engine can be merely represented by functions that relate, for instance, load and speed to specific fuel consumption. This is the so-called transfer function engine model (TFEM), which is the simplest and fastest method. Precisely for these reasons, this sort of modelling is the most suitable for the design optimisation of the ship's overall energy system. Some references in this field are [12, 35] 38]. However, none
reference performed the engine selection optimisation since all models found must be calibrated for each single engine, which is inappropriate for iterative procedures.

### 1.3 Dissertation proposal

The present doctoral dissertation proposes a comprehensive early-stage approach to optimise the design, synthesis, and operation of LNGC energy systems considering economic and technical aspects, besides weather conditions. This approach must assess various configurations of propellers and prime movers to find the best matching and also consider a different number of propulsion chains. The need for a re-liquefaction plant must also be assessed. Constraints must be incorporated in order to avoid propellers that can present issues regarding strength, cavitation, and vibration. This approach must assess different operational profiles, regarding service speeds and fuel, in order to maximise the NPV. This measure of merit considers OPEX, income and capital expenditures (CAPEX).

By using the proposed approach, one is expected to be able to automatically search a broad range of possible alternatives, then make small refinements to achieve the optimal arrangement. Although this can be seen as an extension of what one could theoretically accomplish manually, the labour involved would be prohibitive. Thus, the main contributions of the present work is an engine model suitable to optimise the selection of dual-fuel two-stroke Diesel engines, as well as a comprehensive and integrated approach to optimise the energy system of LNGCs. Furthermore, with some adjustments, the methodology developed herein can apply to any ships.

In the next chapters are presented a brief literature review about LNGC energy systems (Chap. 22), then the development of an engine model suitable for optimisation problems, that is, one that does not need to be calibrated for each engine separately (Chap. 3). Afterwards, it is presented the developed approach (Chap. 4), the case study (Chap. 5), results and discussion (Chap. 6), and lastly the study's conclusions (Chap. 7). Besides, an additional chapter addressing the articles written during the doctoral period and future work proposals is included at the end of this document (Chap. 8).

## Chapter 2

## Literature review

This chapter addresses the main concepts of the most promising propulsion alternatives for LNGCs. Basic knowledge about re-liquefaction plant, environmental regulations and manners of reducing gaseous emissions are included as well. Lastly, alternatives to enhance the performance of the energy system by using the exhaust gas waste heat is presented.

### 2.1 Propulsion alternatives

As an alternative to the steam power plant, there are primarily the gas turbine and the diesel engine power plants, whereas secondarily fuel cells and Stirling engines, as well as renewable energy systems have been studied. Furthermore, combined and co-generation systems have also been used successfully on-board ships [39]. Gas turbine power plants present high power density, the capability to burn BOG and efficiency higher than steam turbine power plants. On the other hand, low redundancy, low efficiency in sea level and its high fuel consumption, as well as the fact of being a relatively untried technology for merchant ships make it a still unsure option. Nowadays, the Diesel engine is the most common prime mover for merchant ships and, with the development of on-board BOG re-liquefaction systems, it became also the most interesting alternative for LNGCs.

### 2.2 Diesel engines

Slow speed two-stroke diesel engines and on-board BOG re-liquefaction system have been used successfully in large LNGCs. A propulsion plant scheme as this one is illustrated in Fig. 2.1 (adapted from [40), where is shown that all the generators and propulsion engines are fed with liquid fuel whereas the BOG is re-liquefied. The generators supply electric power for the re-liquefaction plant and for the other
consumers on-board. Conceptually, the propulsion is separated from the BOG treatment in this case. There is also a gas combustion unit (GCU) in case the BOG amount is greater than the re-liquefaction capacity.


Figure 2.1: Propulsion plant scheme with slow speed two-stroke diesel engine and re-liquefaction plant.

Slow speed Diesel engines driving directly propellers, such as shown in Fig. 2.1, are the arrangement of most of the commercial ships, with proven performance and reliability. However, when conventional liquid fuel prices are higher than LNG price, the OPEX of this propulsion system is increased, as it is unable to use the BOG as fuel. Moreover, regarding environmental controls, conventional fuels are not as clean as the BOG. Thus, an option to overcome these drawbacks is to apply dual-fuel Diesel engines.

### 2.3 Dual-fuel Diesel engines

They are compression ignition engines capable of working with either conventional liquid fuels or gaseous fuels, namely that, in diesel or gas operating mode, respectively. During the diesel mode, these engines work as conventional Diesel engines, burning liquid fuels as heavy fuel oil (HFO), marine diesel oil (MDO) and marine gas oil (MGO), for instance. In the gas mode, a liquid pilot fuel injection is required to start the combustion process.

The specification of medium speed four-stroke dual-fuel Diesel machinery for LNG carrier new buildings in 2002 marked the ousting of steam turbine propulsion in commercial ships [5]. These engines require relatively low pressure (about $6 \mathrm{bar}_{g}$ )
for the BOG to be used as fuel and are applied ordinarily with electric transmission, the reason why is known as dual-fuel Diesel electric (DFDE). It offers high fuel efficiency and freedom of fuel choice between fuel oil and BOG. On the other hand, DFDE systems include high capacity electric switchgear, frequency converters, and electric motors, which require a crew with special skills to maintain.

Figure 2.2 (adapted from [40]) illustrates an example of a DFDE scheme without re-liquefaction plant. In this case, the dual-fuel generators provide electric power for the electric motors, which drive the propeller through a gearbox, and for other consumers on-board. A GCU should be used when BOG is greater than the generators' consumption.


Figure 2.2: DFDE propulsion plant scheme without re-liquefaction plant.
An option to overcome the DFDE drawbacks is to use dual-fuel direct drive (DFDD), in which slow speed two-stroke dual-fuel Diesel engines should be used. They are a recent technology, such that the first LNG carrier fitted with this kind of machinery entered into service in 2016 [41]. Typical values of energy efficiency for DFDD systems can reach about $52 \%$ against $41 \%$ reached with DFDE. Figure 2.3 (adapted from [40]) illustrates a DFDD propulsion plant scheme where all the engines are dual-fuel ones, such that a re-liquefaction plant could be necessary or not, depending on the operational profile of the ship. LNGC energy systems must always include a GCU for the disposal of excess BOG to avoid pressure build-up in the cargo tanks. The use of GCU is typically required during the ship loading and unloading operations and when the BOG demand is low, as well as during the ship cool-down operation when excess BOG is generated.

When a slow speed two-stroke dual-fuel Diesel engine is working in gas mode there are two basic concepts about the gas injection pressure: low pressure (LP) and high pressure (HP). The LP concept illustrated in Fig. 2.4a is based on the premixed lean-burn principle, that is, gaseous fuel is injected into the cylinder at the mid-stroke position, such that an injection pressure below $16 \mathrm{bar}_{g}$ is enough. When


Figure 2.3: DFDD propulsion plant scheme.
the piston is close to the compression stroke end, the air/fuel charge is ignited by a liquid pilot fuel [42]. Differently, the HP concept is based on the diffusion combustion principle, as illustrated in 2.4b, In this case, the gas injection occurs close to the top dead centre, practically at the same time of the pilot fuel injection, such that a pressurised gas injection around $300 \mathrm{bar}_{g}$ is necessary [43].


Figure 2.4: Gas injection pressure concepts for slow speed two-stroke dual-fuel Diesel engines.

### 2.4 Standard selection of slow speed Diesel engines

In order to install the necessary propulsion power, the marine engineer needs details about the ship's resistance as well as the matching propeller/ship load and the delivered engine power [39]. The ship's power requirements, including margins and propeller speed, should be determined. In other words, there must be obtained the specified maximum continuous rating (SMCR), which is the operational point of maximum power at the maximum speed required in the continuous operation of the engine.

Considering engine's brake power and speed are both known at SMCR point, next step on engine selection is acquiring the layout diagram of the entire engines programme from various manufacturers. Then, by placing the SMCR point on them, one could identify every engine of each manufacturer able to supply the required power and speed. Figure 2.5 (adapted from [44]) shows engine layout diagrams of marine slow speed dual-fuel Diesel engines from MAN Diesel \& Turbo Corporation.


Figure 2.5: Layout diagrams of slow speed dual-fuel Diesel engines programme from MAN Diesel \& Turbo.

Next step is determining how many cylinders are necessary through detailed information about each engine. Depending on the number of cylinders, every engine also owns a layout diagram wherein the ratio of power and speed can be selected. It is limited by envelopes defining the area where nominal maximum firing pressure is available for the selection of the SMCR. An engine layout diagram is limited by two lines of constant mean effective pressure (MEP), L1-L3 and L2-L4, and by two constant engine speed lines, L1-L2 and L3-L4, as illustrated in Fig. 2.6 (adapted
from [45]). It is also shown SMCR point and nominal maximum continuous rating (NMCR) point, which is the same as L1.


Figure 2.6: Engine layout diagram of the engine 10S90ME- C9.5-GI.

After listing engines and their number of cylinders to fulfil the requirements, the last step is considering some applicable selection criteria. Among these, technical aspects, as for example engine steady state performance data, can be achieved from engine shop trial measurements as well as by using catalogues. Furthermore, some engine manufacturers provide computational applications as the Computerised Engine Application System - Engine Room Dimensioning (CEAS-ERD) [45].

### 2.5 Re-liquefaction plant

The on-board re-liquefaction system is ideal for long journeys, avoiding BOG losses that are more significant as the journey is longer. Figure 2.7 (adapted from [1]) illustrates an example of turbo-expander refrigeration system for gas liquefaction. This type of system works by compressing and expanding a suitable fluid by the Brayton refrigeration thermodynamic cycle [46]. Typically, $\mathrm{N}_{2}$ or $\mathrm{CH}_{4}$ are used as the working fluid. The main advantages of using $\mathrm{N}_{2}$ is that it is inherently safe and makes the system compact as it does not require any refrigerant storage and make-up. Additionally, starting up and shutting down the plant is quick, venting in an emergency situation is not a safety concern and no flaring is necessary.


Figure 2.7: Re-liquefaction plant scheme.

### 2.6 Exhaust gas emissions

The exhaust gas from marine engines consists largely of $\mathrm{N}_{2}$, oxygen $\left(\mathrm{O}_{2}\right)$, carbon dioxide $\left(\mathrm{CO}_{2}\right)$ and water vapour $\left(\mathrm{H}_{2} \mathrm{O}\right)$, with some small quantities of carbon monoxide ( CO ), sulphur oxides $\left(\mathrm{SO}_{x}\right)$, nitrogen oxides $\left(\mathrm{NO}_{x}\right)$, non-combusted hydrocarbons (HC) and particulate materials (PM). Out of these, $\mathrm{SO}_{x}, \mathrm{NO}_{x}, \mathrm{CO}$, HC and PM are considered noxious or toxic emissions. For some gases, such as $\mathrm{SO}_{x}$ and $\mathrm{CO}_{2}$, the emission ratio is determined by fuel composition. On the other hand, for other gases, namely $\mathrm{NO}_{x}, \mathrm{CO}, \mathrm{HC}$ and PM , the emission ratio is dependent on load and speed of the engine, besides ambient conditions and engine technology.

The International Maritime Organisation (IMO) determines different levels (Tiers) of $\mathrm{NO}_{x}$ control applied based on the ship construction date. Within any particular Tier the actual limit value is determined from the engine rated speed $\left(n_{r}\right)$, as shown in Tab. 2.1 (adapted from [47]). Nonetheless, the Tier III controls apply only to the specified ships while operating in emission control areas (ECAs) established to limit $\mathrm{NO}_{x}$ emissions. Outside such areas, Tier II controls apply. Differently, $\mathrm{SO}_{x}$ and PM emission controls apply to all fuel oil combustion equipment and devices on-board. These controls divide between those applicable inside ECAs and those applicable outside such areas. They are primarily achieved by limiting the maximum sulphur content of the fuel oils. These fuel oil sulphur limits are subject to a series of step changes over the years, as shown in Tab. 2.2 (adapted from [47]).

Table 2.1: $\mathrm{NO}_{x}$ emission limits in $\mathrm{g} / \mathrm{kWh}$.

| Tier | Ship construction date | $n_{r}<130$ | $130 \leq n<2000$ | $n_{r} \geq 2000$ |
| :---: | :---: | :---: | :---: | :---: |
| I | on or after 01/01/2000 | 17.0 | $45 \cdot n^{-0.20}$ | 9.8 |
| II | on or after 01/01/2011 | 14.4 | $44 \cdot n^{-0.23}$ | 7.7 |
| III | on or after 01/01/2016 | 3.40 | $9 \cdot n^{-0.20}$ | 2.0 |

Temperature, time and oxygen concentration are the dominating influences in
the formation of $\mathrm{NO}_{x}$. Hence, the higher the temperature, oxygen concentration and residence time at high temperature in the cylinder, the greater the amount of $\mathrm{NO}_{x}$ created. This explains why low-speed two-stroke engines generate higher $\mathrm{NO}_{x}$ emissions than medium and high-speed four-stroke engines of equivalent power output [5]. That is the reason why as engine speed increases, $\mathrm{NO}_{x}$ limit decreases in Tab. 2.1.

Table 2.2: Fuel oil sulphur limits expressed in percentage by weight

| Outside an ECA | Inside an ECA |
| :---: | :---: |
| $4.5 \%$ prior to 1 January 2012 | $1.5 \%$ prior to 1 July 2010 |
| $3.5 \%$ on and after 1 January 2012 | $1.0 \%$ on and after 1 July 2010 |
| $0.5 \%$ on and after 1 January $2020^{*}$ | $0.1 \%$ on and after 1 January 2015 |

*Depending on the outcome of a review to be concluded by 2018 as to the availability of the required fuel oil, this date could be deferred to 1 January 2025.

### 2.7 Emissions reduction

Apart from the use of alternative fuels, primary and secondary measures can be pursued for reducing $\mathrm{NO}_{x}$ emission levels. The former aims reducing the amount of $\mathrm{NO}_{x}$ formed during combustion by optimising engine parameters, such as valve timing, fuel injection and turbo-charging. In this way, emission levels can be reduced by 30 to $60 \%$. The latter aims removing $\mathrm{NO}_{x}$ from the exhaust gas by downstream cleaning techniques (exhaust gas after-treatment). That way, reductions of over $95 \%$ can be achieved [5]. Some examples of exhaust gas after-treatment concepts are exhaust gas recirculation (EGR) and selective catalytic reduction (SCR).

The EGR concept consists in cooling and cleaning an exhaust gas amount (30 to $40 \%$ ) and recirculate it to scavenge air side [48. Therefore, part of the $\mathrm{O}_{2}$ in scavenge air is replaced by exhaust gas, which is rich in $\mathrm{CO}_{2}$ and $\mathrm{H}_{2} \mathrm{O}$. The effect on $\mathrm{NO}_{x}$ formation is partly due to a reduction of the $\mathrm{O}_{2}$ concentration in the combustion zone, and partly due to the higher heat capacities of $\mathrm{H}_{2} \mathrm{O}$ and $\mathrm{CO}_{2}$. Scavenge air with increased heat capacity reaches lower peak combustion temperature. This method can achieve reduction of 50 to $60 \%$ of $\mathrm{NO}_{x}$ emission, but in return, its reliable operation calls for fuels with low sulphur contents. Figure 2.8 (adapted from [48]) illustrates an engine room arrangement, where there are many types of equipment necessary to make EGR works. This figure shows a tank of caustic soda $(\mathrm{NaOH})$, water treatment unit (WTU), collecting tank unit (CTU) and sludge tank, as well as a scrubber alongside the engine. Freshwater is abbreviated as FW in that figure.


Figure 2.8: Engine room arrangement with EGR.

On the other hand, the SCR process consists in reducing $\mathrm{NO}_{x}$ catalytically in $\mathrm{N}_{2}$ and $\mathrm{H}_{2} \mathrm{O}$ by adding ammonia $\left(\mathrm{NH}_{3}\right)$ as a reducing agent in an SCR reactor [48]. Furthermore, parts of the soot and HC in the exhaust gas are also removed by oxidation in the SCR process reactor. This concept can achieve a reduction of over $90 \%$ of $\mathrm{NO}_{x}$ emission, but in return, its reliable operation also calls for fuels with low sulphur contents. Figure 2.9 (adapted from [48]) illustrates a SCR engine room arrangement, where some additional subsystems are also required. This figure shows a urea tank, a urea supply system, a control system, a vaporiser/mixer and an SCR reactor, as well as a soot blower and a compressor.

Regarding $\mathrm{SO}_{x}$ and PM emission reduction, the simplest solution is burning fuels with low sulphur content. However, fuel oils with low sulphur are more expensive than those of high sulphur; thus, alternative exhaust gas after-treatments have been developed. Chemical and washing/scrubbing desulphurisation processes can remove $\mathrm{SO}_{x}$ and PM from the exhaust gas by bringing it into intensive contact with an alkaline fluid. In open loop systems, the alkaline fluid is seawater (SW) whereas, in closed loop systems, recirculated freshwater (FW) mixed with caustic soda ( NaOH ) is used. These two concepts can be combined in a hybrid installation, such as illustrated in Fig. 2.10 (adapted from [48]).

Just as EGR and SCR, scrubber systems require additional equipment, such as a tank of caustic soda ( NaOH ), a sludge tank, a circulation tank, a water cleaning unit (WCU), a circulation pump and a cooler (Fig. 2.10). Moreover, exhaust gas scrubbers are heavy, need significant installation space and produce large quantities of waste-water and sludge. This water has to be properly treated before discharge into the sea, and the sludge must be disposed of at reception facilities ashore.


Figure 2.9: Engine room arrangement with SCR.

As can be noticed, there are manners to burn low quality and cheap fuels and fulfil the IMO requirements by applying exhaust gas after-treatment equipment. However, all those alternatives bring drawbacks such as voluminous subsystems to be installed in the engine room, use of environmentally unfriendly chemicals, as well as they slightly deteriorate the engine efficiency and increase the $\mathrm{CO}_{2}$ emissions. Therefore, using natural gas as the fuel is the most recommended solution in order to reduce emissions. Its main constituent $\left(\mathrm{CH}_{4}\right)$ contains the highest amount of hydrogen per unit of energy of all fossil fuels. The specific $\mathrm{CO}_{2}$ emissions are typically reduced by $20 \%$ compared with HFO or MDO. The corresponding reduction in $\mathrm{NO}_{x}$ emissions lies between 85 and $90 \%$, whereas $\mathrm{SO}_{x}$ and PM are almost eliminated. Moreover, benzene emissions are reduced by around $97 \%$, there is no visible smoke, no sludge deposits and no lead emissions [5].

### 2.8 Waste heat recovery systems

In order to enhance the overall energy efficiency of a power plant, an option ever more considered is using the waste heat to generate steam and/or power by means of a waste heat recovery system (WHRS). Main engine exhaust gas energy is by far the most attractive among the waste heat sources of a ship because of the heat flow and temperature. Moreover, the exhaust gas heat dissipation accounts for about half of


Figure 2.10: Engine room arrangement with a hybrid system of $\mathrm{SO}_{x}$ scrubber.
the total waste heat, which is about one-fourth of the total fuel energy. In many cases, a WHRS is able to supply the ship's total need of electricity as a standalone power source, but it can also run in parallel with a shaft generator, shaft motor and auxiliary diesel generating sets. This type of advanced power system requires though an advanced power management system [49.

Different principles of WHRS are readily available depending on the level of complexity acceptable to the owner and shipyard and the actual electrical power consumption on-board. Ordinarily, an exhaust gas boiler is used to provide heating steam for ship services, but also there are manners to benefit from that waste heat to provide power. This can be achieved by a power turbine (PT), a steam turbine (ST) or even a combination of both, as shown in Fig. 2.11 (adapted from [49]).


Figure 2.11: Main WHRS principles.

The PT principle consists in an exhaust gas driven turbine connected to a generator via a gearbox. The power turbine is installed on a separate exhaust gas pipe from the exhaust gas receiver, which bypasses the turbochargers. Power equivalent to approximate $3.1 \%$ of the main engine shaft power can be on average achieved by this principle. Similarly, the ST principle consists in a steam driven turbine connected to a generator via a gearbox. The steam is produced in a large exhaust gas driven boiler installed on the main engine exhaust gas piping system. This principle is more efficient and reaches about 5.6 to $6.9 \%$ of the main engine shaft power. On the other hand, an electrical output of over $11 \%$ of the main engine power can only be achieved by utilising a WHRS comprising both steam and power turbines and combined with utilising scavenge air energy for exhaust boiler feed-water heating.

## Chapter 3

## Developed engine model

This chapter proposes a simple and fast model to be used in the selection optimisation of marine slow speed two-stroke dual-fuel Diesel engines. To avoid consulting the catalogue data for every engine, every time the iterative process is carried out, the engine operational features are normalised and the deriving trends are approximated by polynomials.

### 3.1 Methodology

The algorithms for developing the proposed model were implemented in MatLab environment. Owing to the data availability of the web-based application CEAS-ERD, only engines provided by MAN Diesel \& Turbo and covered by this application were studied [45]. Lower heating value has been taken as $42.7 \mathrm{MJ} / \mathrm{kg}$ and $50 \mathrm{MJ} / \mathrm{kg}$ for liquid fuel and gaseous fuel, respectively. Standard ambient conditions provided by the International Organisation for Standardisation (ISO) and sulphur content of $3.5 \%$ were also assumed.

Although engine type designation refers to the number of cylinders, stroke/bore ratio, diameter of piston, engine concept, mark number, fuel injection concept and Tier III technology, narrow engine configurations are studied here. Since all the addressed engines are not equipped with Tier III technology, they hold the same fuel injection concept (GI) $\left.\right|^{11}$ and engine concept (ME-C) $)^{2}$; these appointments are not always repeated. Furthermore, only standard configurations of engines were taken.

[^1]
### 3.1.1 Engine layout diagrams

All necessary information to plot the layout diagrams for the 16 engines considered herein is presented in Tab. 3.1. Brake power per cylinder on the four points of the envelope $\left(P_{B c, L 1}, P_{B c, L 2}, P_{B c, L 3}\right.$ and $\left.P_{B c, L 4}\right)$, speed limits $\left(n_{\min } \text { and } n_{\max }\right)^{3}$ and limitations on the number of cylinders ( $Z_{c, \text { min }}$ and $Z_{c, \text { max }}$ ) are also listed in the table. As it may be noticed, only engines of type G (green ultra-long stroke) and S (super long stroke) were studied.

Table 3.1: Available ME-GI slow speed dual-fuel engines and their particulars to chart layout diagrams.

| Engine | $P_{B c, L 1}$ | $P_{B c, L 2}$ | $P_{B c, L 3}$ | $P_{B c, L 4}$ |  | $n_{\min }$ | $n_{\text {max }}$ |  |  | $Z_{c, \text { min }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |$Z_{c, \text { max }}$.

### 3.1.2 Specific fuel consumption at SMCR

Since specific fuel consumption at SMCR depends on its position on the engine layout diagram, the SMCR was placed on the points L1, L2, L3 and L4 and the operational features of every engine were analysed. Hence, the CEAS-ERD was run four times for every of the 16 engines, summing up 64 runs. Considering the propeller law with loads between 10 and $100 \%$ of SMCR, this application provides a table with specific fuel consumption $[\mathrm{g} / \mathrm{kWh}]$, exhaust gas mass flow $[\mathrm{kg} / \mathrm{s}]$, mixed exhaust gas temperature after turbocharger $\left[{ }^{\circ} \mathrm{C}\right]$ and a guiding steam production capacity of an exhaust gas boiler at $7.0 \mathrm{bar}_{d^{4}}{ }^{4}[\mathrm{~kg} / \mathrm{h}]$.

[^2]Firstly, exhaust gas mass flow (MF) and temperature ( $T$ ) were divided by brake power to obtain specific mass flow (SMF), in $\mathrm{kg} / \mathrm{kWh}$, and specific temperature (ST), in ${ }^{\circ} \mathrm{C} / \mathrm{MW}$, as stated in Eq. 3.1 and 3.2 , respectively. Then, all operational features at SMCR were divided by themselves at NMCR to obtain normalised specific fuel consumptions $\left(\mathrm{SFOC}_{N}, \mathrm{SGC}_{N} \text { and } \mathrm{SPOC}_{N}\right)^{5}$ and normalised specific exhaust gas data $\left(\mathrm{SMF}_{N}\right.$ and $\left.\mathrm{ST}_{N}\right)$ regarding NMCR. Equation 3.3 illustrates this procedure for $\mathrm{SFOC}_{N}$. In these equations, $P_{B}$ is brake power $[\mathrm{kW}]$; the index $i$ varies between 1 and 19 representing engine loads between 10 and $100 \%$ with a step of $5 \%$ of the SMCR; $j$ varies between 1 and 4 representing the SMCR position (L1, L2, L3 and L 4$)$ and $k$ varies between 1 and 16 representing the engines.

$$
\begin{gather*}
S M F_{i j k}=\frac{M F_{i j k}}{P_{B, i j k}} \cdot 3600  \tag{3.1}\\
S T_{i j k}=\frac{T_{i j k}}{P_{B, i j k}} \cdot 1000  \tag{3.2}\\
S F O C_{N, j k}=\frac{S F O C_{S M C R, j k}}{S F O C_{N M C R, k}} \tag{3.3}
\end{gather*}
$$

Polynomial surfaces about specific fuel consumptions at SMCR normalised with respect to NMCR and their percentage errors of regression are illustrated in Fig. 3.1, whilst normalised exhaust gas polynomial surfaces and percentage errors are shown in Fig. 3.2. In both figures, regressions were performed as function of mean effective pressure and engine speed normalised with respect to NMCR (MEP $N_{N}$ and $n_{N}$, as defined by Eq. 3.4 and 3.5, respectively.

$$
\begin{align*}
M E P_{N} & =\frac{M E P_{S M C R}}{M E P_{N M C R}}  \tag{3.4}\\
n_{N} & =\frac{n_{S M C R}}{n_{N M C R}} \tag{3.5}
\end{align*}
$$

Table 3.2 provides the coefficients $(p)$ for every polynomial surfaces formulated as in Eq. 3.6, where $z$ represents $\mathrm{SPOC}_{N}, \mathrm{SGC}_{N}, \mathrm{SFOC}_{N}, \mathrm{SMF}_{N}$ and $\mathrm{ST}_{N}, x$ is $n_{N}$ and $y$ is $\mathrm{MEP}_{N}$.

$$
\begin{equation*}
z=p_{00}+p_{10} \cdot x+p_{01} \cdot y+p_{20} \cdot x^{2}+p_{11} \cdot x \cdot y+p_{02} \cdot y^{2} \tag{3.6}
\end{equation*}
$$

Mean effective pressure may also be written as in Eq. 3.7 [39. Since number of cylinders $\left(Z_{c}\right)$, revolutions of crankshaft per complete working cycle $(r)$ and cylinder swept volume $\left(V_{S}\right)$ are engine constants, $\mathrm{MEP}_{N}$ could also be written as in Eq. 3.8. Hence, $n_{N}$ and $\mathrm{MEP}_{N}$ could be calculated with support of Tab. 3.1.

[^3]Table 3.2: Coefficients of the polynomial surfaces.

| Coefficients | $\mathrm{SPOC}_{N}$ | $\mathrm{SGC}_{N}$ | $\mathrm{SFOC}_{N}$ | $\mathrm{SMF}_{N}$ | $\mathrm{ST}_{N}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $p_{00}$ | 2.297 | 0.7858 | 0.8326 | 1.118 | 7.320 |
| $p_{10}$ | -0.003505 | -0.0003174 | -0.0004246 | -0.3700 | -5.328 |
| $p_{01}$ | -1.295 | 0.2143 | 0.1675 | 0.1291 | -5.883 |
| $p_{20}$ | 0 | 0 | 0 | 0.1533 | 1.552 |
| $p_{11}$ | 0 | 0 | 0 | -0.03078 | 1.548 |
| $p_{02}$ | 0 | 0 | 0 | 0 | 1.791 |

$$
\begin{gather*}
M E P=\frac{r}{Z_{c} \cdot V_{S}} \cdot \frac{P_{B}}{n}  \tag{3.7}\\
M E P_{N}=\frac{P_{S M C R}}{n_{S M C R}} \cdot \frac{n_{N M C R}}{P_{N M C R}} \tag{3.8}
\end{gather*}
$$

As illustrated in Fig. 3.1, normalised specific fuel consumptions vary almost linearly with respect to $\mathrm{MEP}_{N}$ and are practically not influenced by $n_{N}$, hence they could be approached by plans. In contrast, exhaust gas parameters vary with respect to both $\mathrm{MEP}_{N}$ and $n_{N}$, such that plans are not the best approach. Although specific fuel consumptions differ in gas and diesel modes, exhaust gas features are quite similar, thus only one trend of $\mathrm{SMF}_{N}$ and $\mathrm{ST}_{N}$ are shown in Fig. 3.2. Moreover, either engines of type $G$ or $S$ did not present substantial differences and, for this reason, they were analysed together.

It draws attention that the two largest deviations regarding $\mathrm{SFOC}_{N}$ (Fig. 3.1) are around $1.4 \%$, whilst all others do not even reach $0.3 \%$. This is due to engine G40ME-C9.5-GI, which is the only standard fitted with conventional turbocharger instead of high-efficiency turbocharger. On the other hand, the error regarding $\mathrm{SPOC}_{N}$ peaks at $1.8 \%$ and its average is comparably higher. Just as the $\mathrm{SFOC}_{N}$, $\mathrm{SGC}_{N}$ presents only two increased deviations, not above $1.5 \%$, whilst others do not reach $0.3 \%$, which is also due to that engine. On the other hand, only minor deviations peaking at about $0.2 \%$ are noticed regarding SMF $_{N}$ in Fig. 3.2. Similarly, the largest deviation regarding $\mathrm{ST}_{N}$ is under $0.7 \%$.

### 3.1.3 Specific fuel consumption at part load

In this case, after obtaining the specific operational features in different engine loads, they were divided by themselves at SMCR. Hence, the normalised specific fuel consumptions $\left(\mathrm{SFOC}_{S}, \mathrm{SGC}_{S}, \mathrm{SPOC}_{S}\right) b^{6}$ and the normalised specific exhaust gas parameters $\left(\mathrm{SMF}_{S}\right.$ and $\left.\mathrm{ST}_{S}\right)$ with respect to SMCR were acquired. Equation

[^4]

Figure 3.1: Polynomial surfaces of the specific fuel consumptions normalised with respect to NMCR and respective percentage errors of regression.


Figure 3.2: Polynomial surfaces of the exhaust gas parameters normalised with respect to NMCR and respective percentage errors of regression.
[3.9 exemplifies this procedure for $\mathrm{SFOC}_{S}$, where the index $i$ varies between 1 and 19 representing engine loads between 10 to $100 \%$; $j$ varies between 1 and 4 representing the SMCR position and $k$ varies between 1 and 16 representing the engines.

$$
\begin{equation*}
S F O C_{S, i j k}=\frac{S F O C_{i j k}}{S F O C_{S M C R, j k}} \tag{3.9}
\end{equation*}
$$

Table 3.3 provides the coefficients for every polynomial curves formulated as in Eq. 3.10, in which $y$ represents $\mathrm{SPOC}_{S}, \mathrm{SGC}_{S}, \mathrm{SFOC}_{S}, \mathrm{SMF}_{S}$ and $\mathrm{ST}_{S}$, and $x$ is engine load. Every curve was obtained by using centring and scaling transformation to improve the numerical properties of both polynomial and fitting algorithm, hence $x$ is normalised by the mean $(\mu)$ and standard deviation $(\sigma)$ given in Tab. 3.3.

$$
\begin{equation*}
y=p_{0}+p_{1} \cdot x+p_{2} \cdot x^{2}+p_{3} \cdot x^{3}+\ldots+p_{8} \cdot x^{8} \tag{3.10}
\end{equation*}
$$

Since some datasets were approached by more than one polynomial, the letters in Tab. 3.3 ( $\mathrm{a}, \mathrm{b}$ and c ) indicate the load range where the polynomial is suitable. Regarding $\mathrm{SGC}_{N}$, letters indicate respectively ranges from 80 to $100 \%, 35$ to $75 \%$ and 10 to $35 \%$ load. About $\mathrm{SMF}_{N}$ and $\mathrm{ST}_{N}$, "a" indicates a range from 35 to $100 \%$ and "b" from 10 to $30 \%$ load. In addition, Intervals not covered by polynomials could be approximated through linear interpolation.

Table 3.3: Coefficients of the polynomial curves.

| Co. | $\mathrm{SPOC}_{N}$ | $\mathrm{SGC}_{N}$ |  |  | $\mathrm{SFOC}_{N}$ | $\mathrm{SMF}_{N}$ |  | $\mathrm{ST}_{N}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | a | b | c |  | a | b | a | b |
| $p_{0}{ }^{*}$ | 1485 | 984.1 | 956.8 | 973.6 | 991.1 | 1117 | 1564 | 1357 | 4596 |
| $p_{1}{ }^{*}$ | -486.0 | 9.381 | -8.131 | -8.866 | -37.61 | -72.29 | -167.1 | -443.1 | -1349 |
| $p_{2}{ }^{*}$ | 255.6 | 1.295 | 2.578 | 4.834 | 15.05 | -4.884 | 73.82 | 205.3 | 169.8 |
| $p_{3} *$ | -133.9 | 0 | 1.244 | 0 | 20.71 | 3.002 | -56.51 | -69.99 | 0 |
| $p_{4}{ }^{*}$ | -46.64 | 0 | 0 | 0 | -1.715 | 0 | 34.01 | 25.05 | 0 |
| $p_{5}{ }^{*}$ | 35.38 | 0 | 0 | 0 | -10.17 | 0 | 0 | -4.821 | 0 |
| $p_{6}{ }^{*}$ | 49.72 | 0 | 0 | 0 | 2.932 | 0 | 0 | 0 | 0 |
| $p_{7}{ }^{*}$ | -26.17 | 0 | 0 | 0 | 0.7298 | 0 | 0 | 0 | 0 |
| $p_{8}{ }^{*}$ | 0 | 0 | 0 | 0 | -0.1642 | 0 | 0 | 0 | 0 |
| $\mu$ | 55.00 | 90.00 | 55.00 | 22.50 | 55.00 | 67.50 | 20.00 | 67.50 | 20.00 |
| $\sigma$ | 27.39 | 7.082 | 12.92 | 8.550 | 27.39 | 20.16 | 7.077 | 20.16 | 7.077 |

*All coefficient values are multiplied by 1000 .

Polynomial curves for the specific fuel consumptions normalised with respect to SMCR and their percentage errors of regression are shown in Fig. 3.3, whereas normalised exhaust gas polynomial curves and percentage errors are shown in Fig. 3.4. In both figures, regressions were performed as a function of brake power given in percentage of SMCR $\left(P_{B}[\% S M C R]\right)$, which is the same as engine load.

Figure 3.3 shows that $\mathrm{SFOC}_{S}$ presented the minimum value for engine load of $70 \%$. Although there are 64 datasets, they are mostly superimposed such that there are basically four data streams for brake power below $70 \%$ of SMCR. Moreover, the mismatches rise as engine load decreases, such that the greatest error is $1.8 \%$ for $10 \%$ load. Differently, $\mathrm{SPOC}_{S}$ grows steadily as load declines and its error is quite dispersed with a maximum about $1.9 \%$ for $80 \%$ load. Meanwhile, four polynomials were needed to approximate more accurately the behaviour of $\mathrm{SGC}_{S}$, which also presented a global minimum for $70 \%$ load. However, two data streams stand out and the deviation peaks at $-3.3 \%$, whilst all the others reach at most $-1.3 \%$. This is again due to engine G40ME-C9.5-GI, which is the only one fitted with a conventional turbocharger.


Figure 3.3: Polynomial curves of the specific fuel consumptions normalised with respect to SMCR and respective percentage errors of regression.

In order to approach specific exhaust gas mass flow and temperature normalised with respect to $\mathrm{SMCR}\left(\mathrm{SMF}_{S}\right.$ and $\left.\mathrm{ST}_{S}\right)$, three polynomials were applied, as shown in Fig. 3.4. In both cases, wider percentage errors happened for lower loading
conditions, such that for $20 \%$ load the error reached $1.5 \%$ and for $10 \%$ load the error peaked at $5.4 \%$, respectively about $\mathrm{SMF}_{S}$ and $\mathrm{ST}_{S}$.


Figure 3.4: Polynomial curves of the exhaust gas parameters normalised with respect to SMCR and respective percentage errors of regression.

### 3.2 Statement of the model

The model consists of computing the specific fuel consumptions for any operating point, that is, at any engine speed and brake power, by equations such as Eq. 3.11 and 3.12, which exemplify the procedure for SFOC and exhaust gas MF. Any specific fuel consumption can be calculated analogously to SFOC whereas the exhaust gas temperature can be calculated analogously to MF. As one can notice, the procedure to evaluate exhaust gas parameters is different because they were formerly converted into specific variables (divided by brake power). Thus, Eq. 3.12 takes into account brake power at SMCR $\left(P_{B, S M C R}\right)$ and load fraction $\left(f_{S M C R}\right)$. Besides the polynomials previously acquired, the parameter of interest must be known at NMCR in both equations. Thus, Tab. 3.4 lists all necessary information for every engine either in gas or diesel operating mode.

$$
\begin{gather*}
S F O C=S F O C_{N M C R} \cdot S F O C_{N} \cdot S F O C_{S}  \tag{3.11}\\
M F=S M F_{N M C R} \cdot S M F_{N} \cdot S M F_{S} \cdot P_{B, S M C R} \cdot f_{S M C R} \tag{3.12}
\end{gather*}
$$

Table 3.4: Specific features at NMCR for gas and diesel mode.

| Engine | Gas mode |  |  |  | Diesel mode |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | SPOC | SGC | SMF | ST | SFOC | SMF | ST |
|  | $\mathrm{g} / \mathrm{kWh}$ |  | $\mathrm{kg} / \mathrm{kWh}$ | ${ }^{\circ} \mathrm{C} / \mathrm{MW}$ | $\mathrm{g} / \mathrm{kWh}$ | $\mathrm{kg} / \mathrm{kWh}$ | ${ }^{\circ} \mathrm{C} / \mathrm{MW}$ |
| G95-9.5 | 5.0 | 136.7 | 7.943 | 2.863 | 166.0 | 7.965 | 2.911 |
| G90-10.5 | 4.9 | 135.9 | 7.942 | 3.152 | 165.0 | 7.966 | 3.205 |
| S90-10.5 | 5.0 | 136.7 | 7.943 | 3.224 | 166.0 | 7.967 | 3.279 |
| S90-9.5 | 5.0 | 136.7 | 8.040 | 3.385 | 166.0 | 8.065 | 3.442 |
| G80-9.5 | 5.0 | 136.7 | 7.745 | 5.567 | 166.0 | 7.762 | 5.662 |
| S80-9.5 | 5.0 | 136.7 | 8.239 | 5.814 | 166.0 | 8.266 | 5.913 |
| G70-9.5 | 5.0 | 137.5 | 7.739 | 7.933 | 167.0 | 7.764 | 8.070 |
| S70-8.5 | 5.0 | 139.2 | 8.243 | 8.830 | 169.0 | 8.271 | 8.983 |
| S65-8.5 | 5.0 | 139.2 | 8.639 | 10.06 | 169.0 | 8.671 | 10.24 |
| G60-9.5 | 5.0 | 137.5 | 7.942 | 10.77 | 167.0 | 7.959 | 10.96 |
| S60-8.5 | 5.0 | 139.2 | 8.641 | 12.13 | 169.0 | 8.660 | 12.34 |
| G50-9.5 | 5.0 | 138.3 | 7.744 | 14.92 | 168.0 | 7.767 | 15.18 |
| S50-9.5 | 5.0 | 139.2 | 7.640 | 14.42 | 169.0 | 7.663 | 14.67 |
| S50-8.5 | 5.1 | 140.0 | 8.651 | 15.46 | 170.0 | 8.675 | 15.73 |
| G45-9.5 | 5.1 | 140.0 | 7.640 | 21.22 | 170.0 | 7.673 | 21.58 |
| G40-9.5 | 5.2 | 144.1 | 7.364 | 29.09 | 175.0 | 7.364 | 29.55 |

### 3.3 Validation of the model

Two engines of intermediary NMCR were simulated and the results were compared against catalogue data (CEAS-ERD). Since the polynomials were reached considering SMCR on L1, L2, L3 and L4, it is necessary to investigate the model accuracy in intermediate points. Therefore, SMCR was additionally placed in the centre of the engine layout diagram (LC), such that the engine 8G70ME-C9.5-GI was examined for 22.3 MW and 73 rpm , as well as the engine $8 \mathrm{~S} 70 \mathrm{ME}-\mathrm{C} 8.5$-GI was examined for 21.1 MW and 82 rpm .

Figures 3.5 and 3.6 show fuel consumption and exhaust gas parameters from the model compared with catalogue data for the engine 8G70ME-C9.5-GI and 8S70ME-C8.5-GI, respectively. Noticeably, the model is able to predict the behaviour of specific fuel consumptions and exhaust gas with only minor mismatches, even when SMCR is on LC. Although exhaust gas mass flow coincides in diesel and gas mode (MF and $\mathrm{MF}_{\mathrm{d}}{ }^{7}$ ), the temperature in gas mode $\left(T_{g}\right)$ is lower than in diesel mode ( $T$ ) and presents an almost constant difference.

Figures 3.7 and 3.8 illustrate the percentage errors of the model in diesel and gas mode for the engines $8 \mathrm{G} 70 \mathrm{ME}-\mathrm{C} 9.5-\mathrm{GI}$ and $8 \mathrm{~S} 70 \mathrm{ME}-\mathrm{C} 8.5-\mathrm{GI}$, respectively. The

[^5]

Figure 3.5: Fuel consumption and exhaust gas parameters from the model compared with catalogue data for the engine 8G70ME-C9.5-GI.


Figure 3.6: Fuel consumption and exhaust gas parameters from the model compared with catalogue data for the engine 8S70ME-C8.5-GI.
largest deviations about specific fuel oil consumption (SFOC $\underbrace{8}$ ) and exhaust gas temperature ( $T_{e}$ ) occurs for the engine 8G70ME-C9.5-GI when the load is $10 \%$. The former is approximately $1.6 \%$ when SMCR is either on L 2 or L4, and the latter is $-2.4 \%$ when SMCR is on L3, as shown in Fig. 3.7a. The engine 8S70ME-C8.5-GI holds the highest exhaust gas mass flow error $\left(\mathrm{MF}_{e}\right)$, which also come about $10 \%$ load, for SMCR on L3, and accounts for $-0.6 \%$ in Fig. 3.8a.

The biggest errors in gas mode, about specific gas consumption ( $\mathrm{SGC}_{e}$ ), exhaust gas mass flow $\left(\mathrm{MF}_{e}\right)$ and temperature $\left(T_{e}\right)$, occur for $10 \%$ of SMCR whilst the greatest deviation regarding specific pilot oil consumption (SPOCe) takes place when the engine load is $95 \%$. The engine 8G70ME-C9.5-GI holds the highest $\mathrm{SPOC}_{e}$ and $T_{e}$, which are around -2.5 and $-3.4 \%$, as well as happen when SMCR is on LC and L3, respectively (3.7b). On the other hand, 8S70ME-C8.5-GI holds the highest $\mathrm{SGC}_{e}$ and $\mathrm{MF}_{e}$, respectively around -1.1 and $0.6 \%$, and these values happen respectively when SMCR is on L2 and LC, as shown in Fig. 3.8b.


Figure 3.7: Modelling errors for the engine 8G70ME-C9.5-GI.

The results' assessment revealed that the model was not only capable to represent adequately the behaviour of the variables but also presented acceptable percentage errors. The majority of the biggest deviations regarding the two simulated engines occurred for engine load of $10 \%$ and they did not exceed $-3.4 \%$, even when SMCR was placed on the centre of layout diagram. Having this figure as quite acceptable, the model may be utilised successfully when one is interested in exhaust gas mass flow and temperature, as well as specific fuel consumptions. Therefore, a simple and fast model to be applied in optimisation problems about the selection of marine

[^6]

Figure 3.8: Modelling errors for the engine 8S70ME-C8.5-GI.
dual-fuel low-speed diesel engines can be considered developed.

### 3.4 Strengths of the model

The main strengths that make the model suitable for the present purpose are listed following.

+ Only a few input data are required to apply the model, namely: operating engine features in the NMCR, the polynomial surfaces and curves, as well as the power in the SMCR and a load fraction, in case of part load.
+ The model is capable to calculate specific fuel consumptions, exhaust gas mass flow and temperature for every engine working from $10 \%$ to $100 \%$ of SMCR, wherever this point is placed on the envelope.
+ The model presents just small deviations.
+ The processing time is under 0.4 seconds, thereby the model can be considered fast enough.
+ The model is simple and easy to implement, as well as an individual calibration for each engine is unnecessary.


### 3.5 Limitations of the model

Although that model is suitable for the present purpose, some improvements may be incorporated in the future. Thus, in order to guide future works, a list of limitations of the model is presented following.

- Only engines of the type ME-C-GI were used, that is, those whose fuel injection timing and actuation of exhaust valves, starting valves and cylinder lubrication are electronically controlled. Moreover, only engines fitted with high-efficiency turbochargers and without gas after-treatment devices were considered. In other words, only default configurations were used. Thus, Tier III technologies, varied fuel injection concepts, control types, and turbochargers, as well as other optimised load ranges, fuel sulphur contents and ambient conditions could have been taken into account.
- Only engines manufactured by MAN Diesel \& Turbo were included in the study. A broader range of engines could have been used in case other manufacturers provide complete information of their engines.
- As the CEAS-ERD application correlates engine speed with power by the propeller law, the individual effect of them was not accounted. This is an interesting aspect to be enhanced in the future.


## Chapter 4

## Developed approach

Next, it is explained in detail a comprehensive early-stage approach to optimise the synthesis, design and operation of LNGC energy systems. The approach developed in this chapter considers economic and technical aspects, as well as weather conditions, seeking to be minimally complete.

### 4.1 Methodology

In order to set up a comprehensive approach to be used for shipowners and marine engineers, the proposed approach goes over technical and economic aspects as well as considers the weather along the route. Since the net present value (NPV) is a common economic measure of merit, the method consists in an optimisation process whose objective function to be maximised is the NPV and the design variables are propulsion parameters and service speeds. Thus, the purpose is finding the synthesis of components, their design characteristics and the operational profile that maximise the NPV of an LNGC.

Herein, synthesis of components refers to the condition of the propulsion system to hold one or two main engines, each one driving a propeller, and the existence of shipboard re-liquefaction. The components design characteristics refer to the propeller and engine specification. The operational profile refers to the service speed and the fuel to be burnt in each part of the journey, namely the fuel profile. Once a computational environment became necessary, all the computations were performed in MatLab. The proposed approach was explained hereinafter by means of flowcharts and then an overview of each model was addressed.

Figure 4.1 illustrates the proposed approach towards the optimisation of synthesis, design and operation for an LNGC energy system. This figure shows the different computations that were followed, as well as their input and output data. Given a guess of optimisation design variables, that is, propulsion parameters and service speed, the first step is estimating the brake power and shaft speed in service
for each route-track, as detailed in Fig. 4.2. The next steps are computing the specified maximum continuous rating (SMCR) and then determining the suitable engines, still considering the initial guess of design variables. The fourth step is assessing the NPV for each suitable engine considering the different fuel profiles, as detailed in Fig. 4.3. Having accomplished this, it is performed a simple search for the matching of engine and fuel profile that holds the maximum NPV, which is the optimum for that guess of design variables.

All these steps are executed iteratively by the optimisation algorithm, and convergence is verified at the end of each run. If the algorithm converged, the optimum engine-propeller matching was reached; otherwise, a new guess of propulsion parameters is taken by the optimisation algorithm, as detailed in Fig. 4.4. Similarly, if there is no suitable engine among the available options during a run, that initial guess of design variables is considered infeasible, and the optimisation algorithm interrupts the run to guess new design variables and come back to the first step.

In order to estimate brake power and shaft speed in service for each route-track, the procedure shown in Fig. 4.2 was proposed. It starts by computing the total hydrodynamic resistance concerning specified weather conditions and then computing the total resistance in service conditions. Next comes the computation of propulsion factors, followed by calculation of propeller performance. Having accomplished this, technical constraints related to strength, cavitation and vibration are verified. If any of these criteria are not met, the design variables are considered infeasible and the run is interrupted; otherwise, the run proceeds to the computation of brake power in service.

The net present value (NPV) estimation for each matching of engine and fuel profile is achieved by following the procedure illustrated in Fig. 4.3, where is shown the computations and their input and output data. It consists of computing capital expenditures (CAPEX), operational expenditures (OPEX) and then the NPV.

Figure 4.4 shows the iterative procedure of the differential evolution optimisation algorithm applied. It is an evolutionary and stochastic algorithm; in other words, it attempts to mimic nature and does not make use of the gradient of the objective function as a direction of optimisation 50. Firstly, one individual (design) is randomly created by the uniform distribution (continuous) approach 51 and its objective function is assessed. If design variables are infeasible, that individual is rejected and another is created to replace it; otherwise, this individual is kept in the population. This is done until a full population is created, such that there are only capable individuals (feasible design variables) in the initial population. Then, an offspring member is generated from the initial population and its objective function is assessed. If the offspring is better than its main progenitor, it replaces its main


Figure 4.1: Optimisation approach towards synthesis, design and operation of an LNGC energy system.


Figure 4.2: Brake power and shaft speed estimation in service for each route-track.


Figure 4.3: Net present value estimation for each matching of engine and fuel profile.
progenitor in the population; otherwise, the offspring is rejected. This proceeds until every member of the initial population has been the main progenitor of an offspring, that is, until a generation has elapsed. The best member of the population after a predetermined number of generations is considered the optimum design.

### 4.2 Computation of resistance for specified weather conditions

According to CARLTON [52], many approaches can be used to compute total ship resistance in still water, as well as to estimate added resistance due to rough weather. Regarding still water, the usual approach whenever algebraic models are required is the well-known Holtrop-Mennen model [53] [54], which is a statistical power prediction method based on a regression analysis of random model experiments and full-scale test data. Based on geometric parameters and speed, this model provides an approximated value of the total propulsion resistance in still water $\left(R_{T, s w}\right)$.

Owing to the occurrence of rough weather during voyages, the resistance changes and affects the behaviour of the vessel. In order to predict the added resistance, semi-empirical approaches are more suitable than others more complexes in cases where a high computational time is a trouble [25]. The Kwon's model [55] is an approximate method for predicting speed loss of a displacement type ship due to added resistance in weather conditions (irregular waves and wind). The advantage of this method is that it is easy and practical to use once it is based on the Eq. 4.1, where $v_{r w}$ is service speed in rough weather, $v_{s w}$ is service speed in still water, $C_{\beta}$


Figure 4.4: Iterative procedure of the differential evolution optimisation algorithm.
is a direction reduction coefficient, $C_{U}$ is a speed reduction coefficient and $C_{f o r m}$ is a ship form coefficient.

$$
\begin{equation*}
\frac{v_{r w}}{v_{s w}}=1-\frac{C_{\beta} \cdot C_{U} \cdot C_{\text {form }}}{100} \tag{4.1}
\end{equation*}
$$

Since $v_{r w}$ is a design variable in the present work, $v_{s w}$ was calculated by Eq. 4.1 and then the corresponding $R_{T, s w}$ was obtained by Eq. 4.2. In this equation $R_{F}$ is frictional resistance, $1+k_{1}$ is the form factor of the hull, $R_{A P P}$ is appendage resistance, $R_{W}$ is wave resistance, $R_{B}$ is additional pressure resistance of bulbous bow near the water surface, $R_{T R}$ is additional pressure resistance due to transom immersion and $R_{A}$ is the model-ship correlation resistance.

$$
\begin{equation*}
R_{T, s w}=R_{F} \cdot\left(1+k_{1}\right)+R_{A P P}+R_{W}+R_{B}+R_{T R}+R_{A} \tag{4.2}
\end{equation*}
$$

Therefore, one considers that the ship is sailing at $v_{r w}$, which is generally lower than the corresponding $v_{s w}$, but the resistance is that one related to the corresponding $v_{s w}$.

In order to calculate those coefficients, it is necessary to know some parameters related to weather, such as weather direction angle with respect to the ship's bow and Beaufort Number (BN), besides ship parameters and service speed. Weather direction is assumed to be the same as wind (surface waves) and it is also known as encounter angle, such as illustrated in Fig. 4.5. Beaufort Number is used to represent a range of wave heights and sea conditions, which can be taken as a function of the wind speed in $\mathrm{m} / \mathrm{s}$ at a height of 10 m above sea level $\left(v_{10}\right)$, such as illustrated in Eq. 4.3 [56]. Therefore, the monthly means of daily means for zonal and meridional wind components ( 10 metre U wind component and 10 metre V wind component), as well as the absolute wind speed ( 10 metre wind speed) provided by the European Centre for Medium-Range Weather Forecasts [57] was used. There must be noticed that among the measured data supported by this server there are also interpolated data depending on the wished grid.


Figure 4.5: Encounter Angle.

$$
\begin{equation*}
B N=\sqrt[1.5]{\frac{v_{10}}{0.836}} \tag{4.3}
\end{equation*}
$$

### 4.3 Computation of total resistance in service

A well-chosen design condition must be realistic and representative for the service conditions that the ship will encounter during its operational life. Therefore, the total resistance in service ( $R_{T, \text { ser }}$ ) is related to the trial total resistance ( $R_{T, t r i}$ ) by the service margin (SM), as shown in Eq. 4.4. The service margin can be built up as a product of factors including effects of fouling $\left(s m_{f}\right)$, hull form $\left(s m_{h}\right)$, displacement $\left(s m_{d}\right)$, weather $\left(s m_{w}\right)$ and water depth $\left(s m_{w d}\right)$, as illustrated in Eq. 4.5 [39].

$$
\begin{gather*}
R_{T, s e r}=S M \cdot R_{T, t r i}  \tag{4.4}\\
S M=s m_{f} \cdot s m_{h} \cdot s m_{d} \cdot s m_{w} \cdot s m_{w d} \tag{4.5}
\end{gather*}
$$

Herein the effects regarding hull form, displacement and weather have already been taken into account by the previous computation, as well as it is assumed that the ship sails in deep waters most of the time. Hence, the only factor with value different of one is that about fouling $\left(s m_{f}\right)$, which is recommended to take as $3 \%$ of increase resistance per year [39].

### 4.4 Computation of propulsion factors

Only a part of the thrust produced by the propellers is used to overcome the pure towing resistance of a ship, the remaining part has to overcome the added resistance created by the presence of the propellers themselves. Furthermore, the propellers are located within a region where the water velocity is affected by the hull's presence (ship propeller wake). Thus, there must be considered the thrust deduction factor $(t)$ for calculating the thrust (Th), and the wake factor $(w)$ for calculating the advance velocity of the propeller $\left(v_{A}\right)$. These calculations are shown respectively in Eq. 4.6, where $Z_{p}$ is the number of propellers, and Eq. 4.7.

$$
\begin{align*}
& T h=\frac{R_{T, s e r}}{Z_{p} \cdot(1-t)}  \tag{4.6}\\
& v_{A}=(1-w) \cdot v_{r w} \tag{4.7}
\end{align*}
$$

Equations given by Holtrop and Mennen [53] [54], which are based on ship and propeller parameters, as well as on service speed, were applied to obtain these propulsion factors and also the relative rotative efficiency $\left(\eta_{R}\right)$. This latter is used subsequently to calculate brake power in service.

### 4.5 Computation of propeller performance

Over the years there have been a considerable number of standard series propellers tested in many establishments around the world and those most commonly used by propeller designers and analysts are referenced in [52]. Wageningen B-screw series, also known as Troost series, is perhaps the most extensive and widely used propeller series, as declared by the latter author, and for this reason, it was applied. The thrust and torque coefficients ( $K_{T}$ and $K_{Q}$ ) of the screws are expressed as polynomials in the advance ratio $(J)$, the pitch ratio $(P / D)$, the blade-area ratio $\left(A_{E} / A_{O}\right)$ and the number of blades $(Z)$. Additionally, the effect of the Reynolds number $\left(R_{n}\right)$ is taken into account in the polynomials [58]. Thus, the relationships shown in Eq. 4.8 and 4.9 were used to calculate the non-dimensional thrust and torque provided by the propeller.

$$
\begin{align*}
& K_{T}=f_{1}\left(J, P / D, A_{E} / A_{O}, Z, R_{n}\right)  \tag{4.8}\\
& K_{Q}=f_{2}\left(J, P / D, A_{E} / A_{O}, Z, R_{n}\right) \tag{4.9}
\end{align*}
$$

On the other hand, by using open water diagram, the non-dimensional thrust required by the ship ( $K_{T,\}^{1}}{ }^{1}$ ) was calculated by Eq. 4.10. Once $K_{T}$ must equal $K_{T, s}$, the issue is finding the value of $J$ for that, which was made by solving an equation system. Then, shaft speed $(n)$ and torque $(Q)$ were calculated by Eq. 4.11 and Eq. 4.12, respectively, where $\rho$ is the water density and $D$ is the propeller diameter.

$$
\begin{gather*}
K_{T, s}=\frac{T}{\rho \cdot v_{A}^{2} \cdot D^{2}} \cdot J^{2}  \tag{4.10}\\
n=\frac{v_{A}}{J \cdot D}  \tag{4.11}\\
Q=K_{Q} \cdot \rho \cdot n^{2} \cdot D^{5} \tag{4.12}
\end{gather*}
$$

Lastly, open water power $\left(P_{O}\right)$ and efficiency $\left(\eta_{O}\right)$ were obtained respectively from Eq. 4.13 and Eq. 4.14.

$$
\begin{align*}
P_{O} & =2 \pi \cdot Q \cdot n  \tag{4.13}\\
\eta_{O} & =\frac{1}{2 \pi} \cdot \frac{J \cdot K_{T}}{K_{Q}} \tag{4.14}
\end{align*}
$$

[^7]
### 4.6 Constraints

The propulsion design variables were only considered feasible if approved for all criteria, namely propeller blade resistance, cavitation, propeller peripheral velocity, and resonance. Each criterion was tested in that order and more details about them are given below.

### 4.6.1 Propeller blade strength

In order to constrain propellers with unsatisfactory strength properties, the inequality given in Eq. 4.15 was used. The blade thickness at $75 \%$ of the propeller radius $\left(t_{0.75 R}\right)$ must not be lesser than the minimum thickness required $\left(t_{0.75 R, \text { min }}\right)$. Approaches for $t_{0.75 R}$ and $t_{0.75 R, \text { min }}$ given by OOSTERVELD and OSSANNEN [58] were used, as written in Eq. 4.16. This equation is not dimensionally homogeneous, hence $D$ is propeller diameter in $\mathrm{ft}, P_{S}$ is the power delivered by each blade in $\mathrm{hp}, S_{C}$ is the maximum allowable stress of the propeller material in psi and $n$ is propeller speed in rpm.

$$
\begin{equation*}
t_{0.75 R} \geq t_{0.75 R, \min } \tag{4.15}
\end{equation*}
$$

$$
\begin{align*}
& \text { 又 } \cdot(0.0185-0.00125 \cdot Z) \geq \text { Q } \cdot \\
& \quad\left[0.0028+0.21 \cdot \sqrt[3]{\frac{(2375-1125 \cdot P / D) \cdot P_{S}}{4.123 \cdot n \cdot D^{3} \cdot\left(\frac{S_{C}+D^{2} \cdot n^{2}}{12,788}\right)}}\right] \tag{4.16}
\end{align*}
$$

### 4.6.2 Cavitation

Cavitation on back of propeller blades was constrained according to the Burrill cavitation diagram for uniform flow [52] by the inequality given in Eq. 4.17. The thrust loading coefficient $\left(\tau_{c 0.7 R}\right)$ must be at most equal to the maximum thrust loading coefficient ( $\tau_{c 0.7 R, \max }$ ), depending on the maximum cavitation level adopted. By assuming $5 \%$ cavitation as the maximum allowable, the exponential curve shown on the right side of Eq. 4.18 was approximated. On the left side of this equation is shown the definition of thrust loading coefficient. In Eq. $4.18 A_{p}$ is the projected area of the propeller and $\sigma_{0.7 R}$ is the mean cavitation number, which is defined in Eq. 4.19. In this equation, $p_{0}$ is the static pressure at the shaft centre line and $p_{v}$ is the water vapour pressure.

$$
\begin{equation*}
\tau_{c 0.7 R} \leq \tau_{c 0.7 R, \max } \tag{4.17}
\end{equation*}
$$

$$
\begin{gather*}
\frac{T h}{\frac{1}{2} \cdot \rho \cdot A_{p} \cdot\left[v_{A}^{2}+(0.7 \pi \cdot n \cdot D)^{2}\right]} \leq 0.2032 \cdot e^{0.3504 \cdot \sigma_{0.7 R}}-0.2311 \cdot e^{-3.194 \cdot \sigma_{0.7 R}}  \tag{4.18}\\
\sigma_{0.7 R}=\frac{p_{0}-p_{v}}{\frac{1}{2} \cdot \rho \cdot\left[v_{A}{ }^{2}+(0.7 \pi \cdot n \cdot D)^{2}\right]} \tag{4.19}
\end{gather*}
$$

### 4.6.3 Propeller peripheral velocity

The blade tip peripheral velocity ( $v_{\text {tip }}$ ) should be as low as possible in order to reduce noise and vibrations. Its recommended upper level is $39 \mathrm{~m} / \mathrm{s}$ [59], as shown in Eq. 4.20 .

$$
\begin{equation*}
v_{t i p}=\pi \cdot D \cdot n \leq 39 \tag{4.20}
\end{equation*}
$$

### 4.6.4 Resonance

The coincidence of the natural frequency identified with some natural mode and the exciting frequency of some excitation component corresponds to a condition of resonance. Intending to reach ships with consistently acceptable vibration characteristics, it is essential to avoid resonances involving the active participation of major subsystems in frequency ranges where the dominant excitations are strongest [60]. For this reason, attention was given to the hull girder vertical vibration excited by the propeller. Equation 4.21, which is simplified and suitable for initial design stage of ships [61], was applied to calculate the first four orders vertical vibration natural frequencies. In this equation $B$ is the moulded breadth, $D_{m}$ is the moulded depth, $\Delta_{V}$ is the displacement including the virtual added mass of water, $L_{p p}$ is the length between perpendiculars, and $C_{n}$ is a coefficient dependent on vibration order and ship type. This coefficient was approximated as if the ship were a bulk carrier for the three first orders and an extrapolation was carried out to obtain it for the fourth order. The values used for $C_{n}$ are listed in Tab. 4.1.

$$
\begin{equation*}
f_{n}=C_{n} \cdot \sqrt{\frac{B \cdot D_{m}^{2}}{\Delta_{V} \cdot L_{p p}^{2}}} \tag{4.21}
\end{equation*}
$$

Table 4.1: Coefficient $C_{n}$ of the hull girder vertical natural frequency.

| Order | $1^{\text {st }}$ | $2^{\text {nd }}$ | $3^{\text {rd }}$ | $4^{\text {th }}$ |
| :---: | :---: | :---: | :---: | :---: |
| $C_{n}$ | 620.6 | 1212.2 | 1735.6 | 2186.6 |

On the other hand, the excitation frequencies due to the propeller $(f)$ were calculated by Eq. 4.22, in which $n_{h}$ is an integer related to the harmonics ( 1 for the first harmonic and so on).

$$
\begin{equation*}
f=n_{h} \cdot Z \cdot n \tag{4.22}
\end{equation*}
$$

Thus, any propeller that holds excitation frequencies with less than a difference in relation to the hull girder vertical natural frequencies was constrained. Mathematically this corresponds to Eq 4.23 .

$$
\begin{equation*}
0.90 \cdot f_{n} \leq f \leq 1.10 \cdot f_{n} \tag{4.23}
\end{equation*}
$$

### 4.7 Computation of brake power in service

Calculating brake power $\left(P_{B}\right)$ consists in considering losses to approximate the required power in the engine shaft based on the open water power $\left(P_{O}\right)$, as shown in Eq. 4.24. In practice, when a propeller is behind a ship, the power actually delivered to the propeller is generally different from $P_{O}$ as a result of the non-uniform velocity field in front of the propeller. This is offset by the relative rotative efficiency $\left(\eta_{R}\right)$, whilst mechanical losses over the propulsion chain are expressed by shaft efficiency $\left(\eta_{S}\right)$ and gearbox efficiency $\left(\eta_{G B}\right)$.

$$
\begin{equation*}
P_{B}=\frac{P_{O}}{\eta_{R} \cdot \eta_{S} \cdot \eta_{G B}} \tag{4.24}
\end{equation*}
$$

### 4.8 Computation of SMCR

The operating point with the maximum brake power required throughout the journey is taken as the maximum continuous rating (MCR) point. Trying to make sure the ship will be able to keep its service speed and the engine will be not fully loaded even in the hardest condition, margins are considered on the MCR power $\left(P_{M C R}\right)$. Once the service margin (SM) has already been applied, the engine margin (EM), which often lies between 0.8 and 0.9 [39], is used to obtain the SMCR power $\left(P_{S M C R}\right)$, as shown in Eq. 4.25. Meanwhile, the shaft speed at SMCR ( $n_{S M C R}$ ) can be approximated from the shaft speed at MCR $\left(n_{M C R}\right)$ by assuming the propeller law, as shown in Eq. 4.26.

$$
\begin{equation*}
P_{S M C R}=\frac{P_{M C R}}{E M} \tag{4.25}
\end{equation*}
$$

$$
\begin{equation*}
n_{S M C R}=n_{M C R} \cdot \sqrt[3]{\frac{P_{S M C R}}{P_{M C R}}} \tag{4.26}
\end{equation*}
$$

### 4.9 Determination of suitable engines

In order to determine the suitable engines, the standard selection of slow speed Diesel engines (Sec. 2.4) was followed. The first step is placing the SMCR point on the engine layout diagram programme to know which engines are able to supply the required power and speed. Next step is determining how many cylinders are necessary. Thus, a function was implemented to search the suitable engines regarding a given SMCR. To chart diagrams covering the entire capacity of engines, L1 and L3 corresponding to the maximum number of cylinders as well as L2 and L4 corresponding to the minimum number of cylinders were taken from Tab. 3.1. That function plots a chart with all the engine layout diagrams considered and the SMCR point, as sampled in Fig. 4.6.


Figure 4.6: Engine layout diagrams considered and a SMCR of 50 MW and 75 rpm .

Then, another function tests every single engine for speed and those matching the speed are tested for power to predict the required number of cylinders. Thus, a list of suitable engines and their needed number of cylinders to meet the SMCR is provided. Table 4.2 shows the engines and their required number of cylinders for the case from Fig. 4.6. Each one of the four engines could meet the SMCR with different numbers of cylinders, totalling eleven alternatives to be considered.

Only engines covered by the CEAS-ERD [45] were applied herein. This application considers 16 engines (cylinder diameters from 400 to 950 mm ) with a number of cylinders varying between 5 and 12. It represents a total of 83 because

Table 4.2: Suitable engines and number of cylinders.

| Engine | Number of cylinders |
| :---: | :---: |
| G95-9.5 | 8,9 or 10 |
| G90-10.5 | 9,10 or 11 |
| S90-10.5 | 10 or 11 |
| S90-9.5 | 10,11 or 12 |

some engines hold fewer cylinders. All engines are electronically controlled (ME-C engine concept) and are not equipped with exhaust gas after-treatment.

### 4.10 Computation of CAPEX

Among capital expenditures, acquisition costs of the main engine, propeller, shaft and re-liquefaction plant are of primary interest for the present study. Nevertheless, obtaining cost and related data is not easy, as engine manufacturers consider this information confidential. Hence, WATSON [6] decided to use weight as the estimating parameter once it has the advantage to apply to almost all components of ship cost. This author also reached a curve of machinery weight-related cost ( $W R C_{m}$ ), in American dollar [US\$] per tonne [ t ], versus machinery weight $\left(W_{m}\right)$, including materials, labour and overheads. This curve could be approximated by Eq. 4.27, where $W_{m}$ must include the total machinery weight, which is the sum due to the main engine, propeller and shaft. Meanwhile, the re-liquefaction plant was taken as a cargo-related outfit whose weight-related cost ( $W R C_{r p}$ ) is given as being 28500 US\$/t. Therefore, machinery CAPEX ( $C A P E X_{m}$ ) and re-liquefaction plant CAPEX ( $C A P E X_{r p}$ ) were calculated respectively by Eq. 4.28 and 4.29, where $W_{r p}$ is the re-liquefaction plant weight.

$$
\begin{gather*}
W R C_{m}=9850 \cdot e^{-0.001457 \cdot W_{m}}+10226 \cdot e^{-0.00007049 \cdot W_{m}}  \tag{4.27}\\
C A P E X_{m}=W R C_{m} \cdot W_{m}  \tag{4.28}\\
C A P E X_{r p}=W R C_{r p} \cdot W_{r p} \tag{4.29}
\end{gather*}
$$

Once the costs given in [6] are on a 1993 basis, a correction concerning inflation became necessary. In this sense, with respect to oil and gas field machinery and equipment manufacturing, the producer price index industry data was applied [62]. Thus, in order to bring the total CAPEX from a 1993 to a 2015 basis, it was applied Eq. 4.30, where $Z_{p}$ is the number of propulsion chains, PPI stands for producer
price index and $f_{\text {ins }}$ is an installation cost factor.

$$
\begin{equation*}
C A P E X=\left(C A P E X_{m} \cdot Z_{p}+C A P E X_{r p}\right) \cdot \frac{P P I_{2015}}{P P I_{1993}} \cdot f_{\text {ins }} \tag{4.30}
\end{equation*}
$$

Main engine weight was achieved with CEAS-ERD whilst propeller weight ( $W_{p}$ ) and shaft weight $\left(W_{s}\right)$ were respectively approximated by Eq. 4.31 and 4.32 , in which $D$ is propeller diameter in $\mathrm{m}, L_{s}$ is shaft length in $\mathrm{m}, P_{N M C R}$ is power at NMCR in kW and $n_{N M C R}$ is shaft speed at NMCR in rpm [56]. On the other hand, the re-liquefaction plant weight $\left(W_{r p}\right)$ was assumed as 240 t , which is a figure respective to an LNG re-liquefaction system mark III by WARTSILA 63].

$$
\begin{gather*}
W_{p}=D^{3} \cdot\left(0.18 \cdot A_{E} / A_{O}-\frac{Z-2}{100}\right)  \tag{4.31}\\
W_{s}=0.081 \cdot L_{s} \cdot\left(\frac{P_{N M C R}}{n_{N M C R}}\right)^{2 / 3} \tag{4.32}
\end{gather*}
$$

### 4.11 Computation of OPEX

The most representative measures of operational expenditures for the present work are journey cost $\left(C_{j o u}\right)$, purchase cost of the LNG cargo $\left(C_{L N G}\right)$, fuel cost related to propulsion $\left(C_{f, p r o}\right)$, fuel cost related to other consumers on board $\left(C_{f, o t h}\right)$, fuel cost related to BOG re-liquefaction $\left(C_{f, \text { rel }}\right)$, and maintenance cost $\left(C_{m}\right)$. Hence, the total OPEX in a round trip of the vessel is given by Eq. 4.33.

$$
\begin{equation*}
O P E X=C_{j o u}+C_{L N G}+C_{f, p r o}+C_{f, o t h}+C_{f, \text { rel }}+C_{m} \tag{4.33}
\end{equation*}
$$

Journey cost ( $C_{j o u}$ ) includes port fees and tolls. The purchase cost of the LNG cargo ( $C_{L N G}$ ) was calculated by Eq. 4.34 , in which $F O B_{L N G}$ is the free-on-board LNG price, $\rho_{L N G}$ is the LNG density and $V p_{L N G}$ is the cargo volume of LNG purchased at loading terminal. The latter was calculated by Eq. 4.35, where $V t_{L N G}$ is the ship's total cargo capacity in volume, $n_{R T b}$ is the number of route-tracks in ballast, $V_{B O G}$ is the total volume of LNG becoming BOG (including naturally and forced generated amounts), $V_{\text {rel }}$ is the volume of LNG coming from BOG re-liquefaction, $i$ is an index that refers to each route-track in ballast and $V_{h}$ is the heel volume.

$$
\begin{gather*}
C_{L N G}=F O B_{L N G} \cdot V p_{L N G} \cdot \rho_{L N G}  \tag{4.34}\\
V p_{L N G}=V t_{L N G}-V_{h}+\sum_{i=1}^{n_{R T b}}\left[V_{B O G}-V_{r e l}\right]_{i} \tag{4.35}
\end{gather*}
$$

The total fuel costs, either $C_{f, p r o}, C_{f, o t h}$ or $C_{f, r e l}$, must consider the portions referring to fuel oil $\left(C_{f, O}\right)$, pilot oil $\left(C_{f, P O}\right)$ and gaseous fuel $\left(C_{f, G}\right)$, as in Eq. 4.36 . The former is regarding dual-fuel engines when operating in diesel mode, whilst the two latter occur for gas mode. As the gaseous fuel comes from cargo (BOG), its cost is included in $C_{L N G}$, and thereby $C_{f, G}$ was neglected.

$$
\begin{equation*}
C_{f}=C_{f, O}+C_{f, P O}+C_{f, G} \tag{4.36}
\end{equation*}
$$

Regarding fuel cost related to propulsion $\left(C_{f, p r o}\right)$, Eq. 4.37 could be applied to calculate both fuel oil and pilot oil cost. In this equation $C_{f, p L}$ stands for the total liquid fuel cost, $c_{l f}$ is liquid fuel unit cost, SFC is the specific fuel consumption of the prime mover, $\delta t$ is the duration of the condition and the index $i$ refers to each route-track.

$$
\begin{equation*}
C_{f, p L}=c_{l f} \cdot \sum_{i=1}^{n_{R T}}\left[S F C \cdot P_{B} \cdot Z_{p} \cdot \delta t\right]_{i} \tag{4.37}
\end{equation*}
$$

Since there must be a compression system to increase BOG pressure to feed prime mover, the electricity to power this system, other consumers and the re-liquefaction plant is supplied by dual-fuel generation sets. Hence, the cost of liquid fuels to feed other consumers could be calculated by Eq. 4.38, where $S F C_{G E}$ is the specific fuel consumption of the generation engine, $\eta_{G}$ is the generator's efficiency and $P_{o t h}$ is the electric power required by other consumers [23].

$$
\begin{equation*}
C_{f, o L}=c_{l f} \cdot \sum_{i=1}^{n_{R T}}\left[\frac{S F C_{G E}}{\eta_{G}} \cdot P_{o t h} \cdot \delta t\right]_{i} \tag{4.38}
\end{equation*}
$$

In order to calculate the liquid fuel cost for re-liquefying BOG, Eq. 4.39 was used. In this equation, $S P_{B O G}$ is the power required to re-liquefy a mass flow unit of BOG, which is a measure of the specific power requirement of the re-liquefaction plant. Since BOG may be burnt in both prime mover and generation sets, only the surplus is re-liquefied. Therefore, the mass flow of BOG to be re-liquefied ( $\dot{m}_{B O G r}$ ) in each route-track was calculated by Eq. 4.40. The flow of naturally generated BOG ( $\dot{m}_{B O G g}$ ) and of total consumed BOG ( $\dot{m}_{B O G c}$ ) are given by Eq. 4.41 and 4.42, respectively. In these equations, $V_{L N G}$ is the volume of LNG in the tanks for each route-track, BOR is the boil-off rate and $P_{\text {com }}$ is the electric power required by the BOG compression system. Such equations were solved iteratively because the BOG consumed to re-liquefy the surplus of BOG also reduces the amount of BOG to be re-liquefied.

$$
\begin{equation*}
C_{f, r L}=c_{l f} \cdot \sum_{i=1}^{n_{R T}}\left[\frac{S F C_{G E}}{\eta_{G}} \cdot S P_{B O G} \cdot \dot{m}_{B O G r} \cdot \delta t\right]_{i} \tag{4.39}
\end{equation*}
$$

$$
\begin{gather*}
\dot{m}_{B O G r}=\dot{m}_{B O G g}-\dot{m}_{B O G c}  \tag{4.40}\\
\dot{m}_{B O G g}=V_{L N G} \cdot \rho_{L N G} \cdot B O R  \tag{4.41}\\
\dot{m}_{B O G c}=S G C \cdot P_{B} \cdot Z_{p}+\frac{S G C_{G E}}{\eta_{G}} \cdot\left(P_{o t h}+P_{c o m}+S P_{B O G} \cdot \dot{m}_{B O G r}\right) \tag{4.42}
\end{gather*}
$$

Noticeably, all fuel costs are strongly dependent on the specific fuel consumption of the prime mover and generation sets. To assess the specific fuel consumption of the dual-fuel low-speed Diesel engines, the engine model herein-before developed in Chap. 3 is used. More precisely, the statement of the model is addressed in Sec. 3.2 .

The total maintenance cost $\left(C_{m}\right)$ includes propeller and prime mover. However, as the maintenance cost of a propeller is significantly lower than that of an engine, only the engine maintenance cost $\left(C_{m, E}\right)$ was taken into account. To calculate it, one used Eq. 4.43.

$$
\begin{equation*}
C_{m} \approx C_{m, E}=c_{m} \cdot \sum_{i=1}^{n_{R T}}\left[P_{N M C R} \cdot Z_{p} \cdot \delta t\right]_{i} \tag{4.43}
\end{equation*}
$$

### 4.12 Computation of NPV

As implied by its name, NPV is simply the present value of the projected cash flow including the investments. It requires an estimate of future revenues and it assigns an interest rate for discounting future, usually after-tax, cash flows [7. Thus, NPV was calculated by Eq. 4.44 , where $n_{y}$ is the period of economic analysis in years (the ship's lifetime), $F y$ is the annual net cash flow, $r_{d}$ is the discount rate and $i$ is an index that refers to each year of economic analysis.

$$
\begin{equation*}
N P V=\sum_{i=1}^{n_{y}}\left[\frac{F y}{\left(1+r_{d}\right)^{i}}-C A P E X\right]_{i} \tag{4.44}
\end{equation*}
$$

The annual net cash flow $F y$ is given by the difference between income and OPEX, being calculated by Eq. 4.45, in which $n_{r n d}$ is the number of round trips a year, $C I F_{L N G}$ is the cost-insurance-freight LNG price and $V d_{L N G}$ is the volume of LNG delivered at unloading terminal. The latter was calculated by Eq. 4.46, where $n_{R T l}$ is the number of route-tracks in laden and the index $i$ refers to each route-track in laden.

$$
\begin{gather*}
F y=\sum_{i=1}^{n_{r n d}}\left[C I F_{L N G} \cdot V d_{L N G} \cdot \rho_{L N G}-O P E X\right]_{i}  \tag{4.45}\\
V d_{L N G}=V t_{L N G}-V_{h}-\sum_{i=1}^{n_{R T l}}\left[V_{B O G}-V_{r e l}\right]_{i} \tag{4.46}
\end{gather*}
$$

### 4.13 Differential evolution optimisation algorithm

In this algorithm the generation of an offspring member $\left(P_{i, j+1}\right)$ is given by Eq. 4.47, where $P_{i, j}$ is the $i^{\text {th }}$ individual of the $j^{\text {th }}$ generation of the population $\Pi ; \alpha, \beta$ and $\gamma$ are three randomly chosen members of the population $\Pi ; F$ is a weight constant, which defines the mutation $(0.5 \leq F \leq 1.0)$; $\delta_{1}$ and $\delta_{2}$ are two functions related to crossover. Depending on the value of a random number $R$ (between 0 and 1) and of the crossover factor $C R(0.5 \leq C R \leq 1.0), \delta_{1}$ and $\delta_{2}$ take different values, such as shown in Eq. 4.48 .

$$
\begin{align*}
& P_{i, j+1}=\delta_{1} \cdot P_{i, j}+\delta_{2} \cdot\left[P_{\alpha, j}+F \cdot\left(P_{\beta, j}-P_{\gamma, j}\right)\right]  \tag{4.47}\\
& \text { if } R \leq C R\left\{\begin{array} { l } 
{ \delta _ { 1 } = 0 } \\
{ \delta _ { 2 } = 1 }
\end{array} \quad , \text { otherwise } \left\{\begin{array}{l}
\delta_{1}=1 \\
\delta_{2}=0
\end{array}\right.\right. \tag{4.48}
\end{align*}
$$

The random generation of integers was achieved by considering uniformly distributed pseudo-random integers. Meanwhile, the generation of floats was done by considering uniformly distributed random numbers [51].

## Chapter 5

## Case study

This chapter addresses the ship and energy system parameters adopted to test the relevance of the developed approach. Details about the route, operational profiles, as well as economic and optimisation issues, are also included.

### 5.1 Ship

The case study of an LNGC with a cargo capacity of $175,000 \mathrm{~m}^{3}$ was proposed and its hull for the specific situation of two propellers is illustrated in Fig. 5.1. This ship holds the parameters listed in Tab. 5.1. As one may notice, various parameters are different for laden and ballast operation whilst others do not vary.


Figure 5.1: LNGC for the case study.

The energy system of the ship is schematically shown in Fig. 5.2, where it can be noticed that BOG can feed the GCU, the dual-fuel generation sets, the BOG compression system and the re-liquefaction plant. On the other hand, dual-fuel generation sets provide electricity to re-liquefaction plant, other consumers and BOG compression system. The existence of a re-liquefaction system is not mandatory,

Table 5.1: Ship parameters.

| Parameter | Symbol | Unit | Laden | Ballast |
| :---: | :---: | :---: | :---: | :---: |
| Length on waterline | $L$ | m | 292.7 | 282.3 |
| Length between perpendiculars | $L_{p p}$ | m | 293.7 |  |
| Moulded breadth | $B$ | m | 49.00 |  |
| Moulded draught | $T_{m}$ | m | 11.50 |  |
| 9.500 |  |  |  |  |
| Moulded depth | $D_{m}$ | m | 23.00 |  |
| Moulded displacement volume | $\nabla$ | $\mathrm{m}^{3}$ | 118,464 | 95,511 |
| Longitudinal centre of buoyancy | LCB | $\%$ | -1.951 | 0.1984 |
| Transverse bulb area | $A_{B T}$ | $\mathrm{~m}^{2}$ | 25.00 |  |
| Centre of bulb area above keel line | $h_{B}$ | m | 5.300 |  |
| Midship section coefficient | $C_{M}$ | - | 0.9856 | 0.9825 |
| Water-plane area coefficient | $C_{W P}$ | - | 0.8160 | 0.8125 |
| Stern shape parameter | $C_{\text {stern }}$ | - | -25 |  |

such that the ship can hold it or not. Likewise, the ship can have two propulsion chains or only one, as shown in that figure.


Figure 5.2: Energy system scheme.

Table 5.2 lists the energy system parameters for the studied ship. Some data, namely $\mathrm{SP}_{B O G}, P_{\text {oth }}$ and $P_{\text {com }}$, were achieved by regression from [23]. The $S F O C_{G E}, S G C_{G E}, S P O C_{G E}$ and $\eta_{G}$ were achieved by considering generation sets with engines W34DF of 435 kW per cylinder [64]. Since the composition of BOG is time-dependent, an average value for $L H V_{B O G}$ was taken from [2].

The values of all specific fuel consumptions, including those from the engine model developed herein-before (Chap. 3), were taken regarding standard lower heating values of $42,700 \mathrm{~kJ} / \mathrm{kg}$ and $50,000 \mathrm{~kJ} / \mathrm{kg}$, respectively for liquid ( $L H V_{l}$ ) and gaseous fuel $\left(L H V_{g}\right)$. They must thereby be rectified regarding $\mathrm{LHV}_{H F O}$ and $\mathrm{LHV}_{B O G}$. Assuming the engine efficiency as a constant regarding fuels of the

Table 5.2: Energy system parameters.

| Parameter | Symbol | Unit | Value |
| :---: | :---: | :---: | :---: |
| Centre of propeller shaft above keel line | $h_{s}$ | m | 4.250 |
| Shaft length from engine to propeller | $L_{s}$ | m | 30.00 |
| Total cargo capacity | $V t_{L N G}$ | $\mathrm{~m}^{3}$ | 175,000 |
| Shaft efficiency | $\eta_{S}$ | $\%$ | 99.00 |
| Fouling factor | $s m_{f}$ | - | 1.075 |
| Engine margin | EM | $\%$ | 90.00 |
| Re-liquefaction plant weight | $W_{r p}$ | t | 240.0 |
| Boil-off rate | $\mathrm{BOR}^{2}$ | $\%$ | 0.150 |
| Heel volume fraction | $r_{h}$ | $\%$ | 5.000 |
| LNG density | $\rho_{L N G}$ | $\mathrm{t} / \mathrm{m}^{3}$ | 0.427 |
| Re-liquefaction specific power (laden) | $\mathrm{SP}_{B O G, l}$ | $\mathrm{kWh} / \mathrm{t}$ | 831.6 |
| Re-liquefaction specific power (ballast) | $\mathrm{SP}_{B O G, b}$ | $\mathrm{kWh} / \mathrm{t}$ | 4550 |
| Electric power of other consumers | $P_{o t h}$ | kW | 2121 |
| Electric power of BOG compression | $P_{c o m}$ | kW | 1630 |
| SFOC of generation engines | $\mathrm{SFOC}_{G E}$ | $\mathrm{~g} / \mathrm{kWh}$ | 189.0 |
| SGC of generation engines | $\mathrm{SGC}_{G E}$ | $\mathrm{~g} / \mathrm{kWh}$ | 152.6 |
| SPOC of generation engines | $\mathrm{SPOC}_{G E}$ | $\mathrm{~g} / \mathrm{kWh}$ | 2.000 |
| Generator efficiency | $\eta_{G}$ | $\%$ | 96.00 |
| HFO lower heating value | $L H V_{H F O}$ | $\mathrm{~kJ} / \mathrm{kg}$ | 40,500 |
| MGO lower heating value | $L H V_{M G O}$ | $\mathrm{~kJ} / \mathrm{kg}$ | 42,700 |
| BOG lower heating value | $\mathrm{LHV} B O G$ | $\mathrm{~kJ} / \mathrm{kg}$ | 46,000 |

same phase (gaseous or liquid), the specific fuel consumption becomes inversely proportional to the LHV. Hence, Eq. 5.1 was used to find the specific heavy fuel oil consumption (SFOC $C_{H F O}$ ) from the specific fuel oil consumption (SFOC) for $\mathrm{LHV}_{l}$. The specific pilot heavy fuel oil consumption (SPOC $C_{H F O}$ ) was analogously calculated. Similarly, the specific BOG consumption $\left(S G C_{B O G}\right)$ was calculated from the specific gas consumption (SGC) for $\mathrm{LHV}_{g}$ using Eq. 5.2.

$$
\begin{align*}
S F O C_{H F O} & =S F O C \cdot \frac{L H V_{l}}{L H V_{H F O}}  \tag{5.1}\\
S G C_{B O G} & =S G C \cdot \frac{L H V_{g}}{L H V_{B O G}} \tag{5.2}
\end{align*}
$$

### 5.2 Route

This ship travels in laden from Lake Charles to Tokyo Bay via Panama Canal, and returns in ballast, following the great circle route, as shown in Fig. 5.3. This is the shortest course between two points on the surface of a sphere and that is why it was used. The topology of the monthly average wind speed for December 2015 is presented in the same figure. Twenty way-points were considered, dividing the route into 19 tracks. Table 5.3 presents the route parameters of interest for each route-track (RT), where $S$ is the route-track length whilst BN and $\theta_{l}$ are 2015 average values respectively concerning Beaufort Number and encounter angle for the laden trip. It is worthwhile to notice that the encounter angle for ballast trip is the supplementary angle of $\theta_{l}$.


Figure 5.3: Route between Lake Charles and Tokyo Bay via Panama Canal and the topology of absolute wind speed [m/s] for December 2015.

Table 5.3: Route parameters.

| RT | $\mathrm{S}[\mathrm{km}]$ | BN | $\theta_{l}\left[^{\circ}\right]$ |
| :---: | :---: | :---: | :---: |
| $1-2$ | 59.0 | 3 | 64.78 |
| $2-3$ | 1339 | 4 | 47.70 |
| $3-4$ | 1339 | 4 | 83.55 |
| $4-5$ | 77.0 | 3 | 132.4 |
| $5-6$ | 1015 | 3 | 58.33 |
| $6-7$ | 1015 | 3 | 142.8 |
| $7-8$ | 1015 | 2 | 42.50 |
| $8-9$ | 1015 | 3 | 52.42 |
| $9-10$ | 1015 | 4 | 40.52 |
| $10-11$ | 1015 | 4 | 48.76 |
| $11-12$ | 1015 | 4 | 65.82 |
| $12-13$ | 1015 | 4 | 50.10 |
| $13-14$ | 1015 | 5 | 36.69 |
| $14-15$ | 1015 | 5 | 7.438 |
| $15-16$ | 1015 | 5 | 0.561 |
| $16-17$ | 1015 | 5 | 12.30 |
| $17-18$ | 1015 | 5 | 23.21 |
| $18-19$ | 1015 | 5 | 50.71 |
| $19-20$ | 93.0 | 3 | 74.54 |

### 5.3 Operational profile

The ship keeps a different operational profile regarding service speed and fuel to burn depending on the stage of the route, as presented in Tab. 5.4. Three levels of service speed were identified to reduce pollution, such that the smaller the distance from a continent, the slower the speed. Thus, the three levels were: low for $v_{r w} \leq 12.0$ knots [kn], intermediary for $v_{r w} \leq 16.0 \mathrm{kn}$ and high for $v_{r w} \leq 19.5 \mathrm{kn}$. Moreover, since cleaner fuels must be burnt between way-points 1 and 5 , as well as between 19 and 20 due to environmental rules, four fuel profiles (FPs) were proposed:

1. Prime mover and generation sets burn HFO wherever possible and MGO only where is necessary, such that BOG is completely re-liquefied.
2. Prime mover and generation sets burn HFO wherever possible and BOG only where is necessary, such that only the remaining BOG is re-liquefied. In this case, wherever BOG is applied the pilot oil is MGO.
3. Prime mover and generation sets burn only BOG in laden whilst in ballast they burn HFO wherever possible and MGO where is necessary, such that only the remaining BOG is re-liquefied. In this case, pilot oil is always MGO for the generation sets whilst the prime mover uses HFO wherever is possible and MGO only where cleaner fuels are required.
4. Prime mover and generation sets only burn BOG during the entire voyage, such that there is no re-liquefaction plant and the remaining BOG is burnt in a gas combustion unit (GCU). Pilot oil is always MGO for the generation sets whilst the prime mover uses HFO wherever is possible and MGO only where cleaner fuels are required.

Table 5.4: Operational profile.

| RT | $\begin{gathered} v_{r w} \\ \mathrm{kn} \end{gathered}$ | $\mathrm{FP}_{1}$ | $\mathrm{FP}_{2}$ | $\mathrm{FP}_{3}$ | $\mathrm{FP}_{4}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1-5 | $\leq 12.0$ | MGO | BOG/MGO | BOG/MGO | BOG/MGO |
| 5-11 | $\leq 16.0$ | HFO | HFO | BOG/HFO(MGO) | BOG/HFO(MGO) |
| 11-18 | $\leq 19.5$ | HFO | HFO | BOG/HFO(MGO) | BOG/HFO(MGO) |
| 18-19 | $\leq 16.0$ | HFO | HFO | BOG/HFO(MGO) | BOG/HFO(MGO) |
| 19-20 | $\leq 12.0$ | MGO | BOG/MGO | BOG/MGO | BOG/MGO |
| 20-19 | $\leq 12.0$ | MGO | BOG/MGO | MGO | BOG/MGO |
| 19-18 | $\leq 16.0$ | HFO | HFO | HFO | BOG/HFO(MGO) |
| 18-11 | $\leq 19.5$ | HFO | HFO | HFO | BOG/HFO(MGO) |
| 11-5 | $\leq 16.0$ | HFO | HFO | HFO | BOG/HFO(MGO) |
| 5-1 | $\leq 12.0$ | MGO | BOG/MGO | MGO | BOG/MGO |

Note: the ship sails in laden from 1 to 20 and in ballast from 20 to 1 .

Although the total time of a round trip depends mainly on the service speeds, a constant standing period of 24 hours in each port for loading and unloading was also considered. Moreover, this ship has an idle time of 14 days for dry-docking or afloat repairs every 2.5 years, which is important to calculate the average number of round trips a year $\left(n_{r n d}\right)$ and to estimate the fouling service margin $\left(s m_{f}\right)$.

### 5.4 Economic and optimisation parameters

Table 5.5 presents the economic parameters, where $C_{\text {jou }}$ includes only the port fees and Panama Canal tolls over a round trip. The optimisation variables and their ranges are listed in Tab. 5.6. The last five rows contain the only discrete variables whereas the others are continuous. Moreover, the last three variables are the only secondary ones, such that they are not input data, they are dependent on the others and are achieved by running the optimisation algorithm although they are also optimised. Besides the optimisation variables, it is important to mention the factors related to mutation $(F)$ and crossover (CR), which equal 0.8 and 0.5 , respectively.

Table 5.5: Economic parameters.

| Parameter | Symbol | Unit | Value |
| :---: | :---: | :---: | :---: |
| Producer price index 1993 | $\mathrm{PPI}_{1993}$ | - | 138.4 |
| Producer price index 2015 | $\mathrm{PPI}_{2015}$ | - | 267.9 |
| Installation cost factor | $f_{\text {ins }}$ | - | 2.0 |
| HFO unit cost | $c_{H F O}$ | $\mathrm{US} \$ / \mathrm{t}$ | 314.2 |
| MGO unit cost | $c_{M G O}$ | $\mathrm{US} \$ / \mathrm{t}$ | 547.3 |
| Cost-insurance-freight LNG price | $\mathrm{CIF}_{L N G}$ | $\mathrm{US} \$ / \mathrm{t}$ | 550.8 |
| Free-on-board LNG price | $\mathrm{FOB}_{L N G}$ | $\mathrm{US} \$ / \mathrm{t}$ | 371.8 |
| Maintenance unit cost | $c_{m}$ | $\mathrm{US} \$ / \mathrm{kWh}$ | $1.6 \cdot 10^{-3}$ |
| Journey cost a round trip | $C_{j o u}$ | $\mathrm{US} \$$ | 979,724 |
| Discount rate | $r_{d}$ | $\%$ | 9.0 |
| Period of economic analysis | $n_{y}$ | y | 20 |

Table 5.6: Optimisation variables.

| Variable | Symbol | Unit | Range |
| :---: | :---: | :---: | :---: |
| Low service speed (laden) | $v_{r w, l l}$ | kn | $10.0-12.0$ |
| Intermediary service speed (laden) | $v_{r w, i l}$ | kn | $12.0-16.0$ |
| High service speed (laden) | $v_{r w, h l}$ | kn | $16.0-19.5$ |
| Low service speed (ballast) | $v_{r w, l b}$ | kn | $10.0-12.0$ |
| Intermediary service speed (ballast) | $v_{r w, i b}$ | kn | $12.0-16.0$ |
| High service speed (ballast) | $v_{r w, h b}$ | kn | $16.0-19.5$ |
| Propeller diameter | $D$ | m | $6.50-8.50$ |
| Expanded area ratio | $A_{E} / A_{O}$ | - | $0.30-1.05$ |
| Pitch ratio | $P / D$ | - | $0.50-1.40$ |
| Number of blades | $Z$ | - | $2-7$ |
| Number of propulsion chains | $Z_{p}$ | - | $1-2$ |
| Engine identification | $E_{I D}$ | - | $1-16$ |
| Number of cylinders | $Z_{c}$ | - | $5-12$ |
| Fuel profile identification | $F P_{I D}$ | - | $1-4$ |

## Chapter 6

## Results and discussion

Next, it is presented the influence of the optimisation algorithm parameters on the NPV along the generations. The evolution of each variable and the effectiveness of the constraints are assessed as well as the engine and fuel profile selection effect. Ultimately, the weather condition effect is discussed.

### 6.1 Optimization algorithm parameters

Firstly, it was necessary to verify if the population size $\left(n_{P}\right)$ and the number of generations $\left(n_{G}\right)$ used were suitable. The convergence of optimisation is heavily dependent on these parameters and their ideal values are specific to every single case. Therefore, three combinations of these parameters were assessed by plotting the maximum, mean and minimum of the objective function throughout the generations, as shown in Fig. 6.1.

By comparing Fig. 6.1a and Fig. 6.1b, one can notice that doubling the number of generations had a small effect on the objective function. Even less influential was to double the population size, as can be seen when comparing Fig. 6.1b and Fig. 6.1c. Thus, a population of 120 individuals and 120 generations (Fig. 6.1c) were considered suitable. The processing times for a computer fitted with a processor Intel Core i7-5930K of 3.50 GHz and 16 GB of RAM were $1.6,2.7$ and 5.9 h , respectively for the case (a), (b) and (c). The worst individual of the final population, in comparison with the worst individual of the initial population, had the objective function (NPV) increased by $21 \%, 20 \%$ and $22 \%$ respectively for the case (a), (b) and (c).


Figure 6.1: Optimisation algorithm convergence for different values of $n_{P}$ and $n_{G}$.

### 6.2 Optimisation summary

Table 6.1 shows the optimisation summary, where one can see the effectiveness of the constraints and a number of computations performed by the algorithm. Remarkably, almost $48 \%$ of the 15,023 configurations assessed by the algorithm were constrained. The peripheral velocity constraint was responsible for over $33 \%$ of the rejected designs whereas cavitation was responsible for over $31 \%$, engine for $18 \%$, strength for $13 \%$ and the resonance constraint was responsible for under $4 \%$. This table shows also some remarks about the optimisation process.

Overall, 623 designs were assessed to create the initial population, which means that 1 out of each 5.192 was feasible, and each offspring member took on average 1.4 s to be generated. Furthermore, some particularities were noticed about the designs rejected due to each constraint. Over $75 \%$ of the designs rejected due to the strength constraint presented in combination: high service speed ( $v_{r w, h}$ ), number of blades $(Z)$ greater than or equal to six and only one propulsion chain $\left(Z_{p}\right)$. Nevertheless, as $99 \%$ of these rejected designs presented $Z \geq 6$, the number of blades was the most influential parameter. Similar remarks are presented for each constraint in Tab. 6.1. Since $64 \%$ of the designs rejected due to the cavitation constraint had $A_{E} / A_{O}<$ 0.675 and almost $80 \%$ of those rejected due to peripheral velocity had $A_{E} / A_{O}>$ 0.675 , there is no general advice about the best value for expanded area ratio. The same occurs for other parameters, such that there is no general advice about the propeller configuration, which highlights the usefulness of the proposed approach.

Figure 6.2 shows the evolution of the fourteen optimisation variables for the best individual of each generation. As one may observe, almost all parameters presented a significant variation range and all of them were steady from the $86^{\text {th }}$ generation until the end. Various engines $\left(2 \leq E_{I D} \leq 13\right)$ with various numbers of cylinders ( $5 \leq Z_{c} \leq 9$ ) were the best one depending on the generation. On the other hand, fuel profile $\left(\mathrm{FP}_{I D}\right)$ was the only variable that remained steady throughout

Table 6.1: Optimisation summary.

| Designs | Used/Rejected | Remarks |
| :---: | :---: | :---: |
| 623 | used to create initial population | feasibility ratio of 1 to 5.192 |
| 14,400 | used to generate all offspring generations | generation ratio of 1 offspring member to each 1.413 s |
| 931 | rejected due to strength constraint | 829 designs for $v_{r w, h}, 923$ for $Z \geq 6,811$ for $Z_{p}=1$ and 701 combined these aspects |
| 2252 | rejected due to cavitation constraint | 1443 designs for $A_{E} / A_{O}<0.675$ |
| 2428 | rejected due to peripheral velocity constraint | 2159 designs for $v_{r w, h}, 1940$ for $A_{E} / A_{O}>0.675,2351$ for $P / D<$ 0.95 and 1667 combined these aspects |
| 275 | rejected due to resonance constraint | 269 designs for $v_{r w, l}, 263$ for $Z \leq$ 3, 236 for $P / D>0.95,218$ for $Z_{p}=2$ and 171 combined these aspects |
| 1286 | rejected due to engine constraint | no |

the generations. This is due to the strong relationship between fuel profile and fuel unit cost, which was not changed. Since in the $\mathrm{FP}_{2}$ the ship uses the fuel of lowest unit cost (HFO) wherever possible and the second cheaper fuel (BOG) only where is necessary, this fuel profile was always optimum.


Figure 6.2: Evolution of the optimisation variables throughout the generations.

Table 6.2 presents average $(\mu)$ and standard deviation $(\sigma)$ for the optimisation variables and also four alternatives of synthesis, design and operation (SDO) from
the final population. The variables $v_{r w, l l}, v_{r w, i l}, v_{r w, l b}, v_{r w, i b}$ and $D$ presented average values close to their upper limits and low $\sigma$, indicating a trend. Similarly, $Z_{p}$ trended to its lower limit, that is, one engine driving directly one propeller. $\mathrm{FP}_{I D}$ presented $\sigma$ equals zero because there was no variation regardless the other variables, as previously explained and illustrated in Fig. 6.2.

The $\mathrm{SDO}_{1}$ and $\mathrm{SDO}_{4}$ in Tab. 6.2 are respectively the best (optimum) and the worst alternative, whereas the others are randomly chosen intermediates. $E_{I D} 7,8$ and 12 stand respectively for the engines G70-9.5, S70-8.5 and G50-9.5 [65], thus a considerable diversity in size, weight and power per cylinder is observed in the final population. Although there are quite distinct individuals, the optimisation results for each SDO are close, indicating that the population is well-converged.

In order to assess propeller and engine performance, Eq. 6.1 and Eq. 6.2 were used to calculate an average open water efficiency ( $\eta_{O, \text { avg }}$ ) and an average engine efficiency ( $\eta_{E, \text { avg }}$ ), respectively. Remarkably, the best design does not hold the most efficient either propeller or engine. Contrarily, the $\mathrm{SDO}_{4}$ holds the highest $\eta_{O, \text { avg }}$ and the $\mathrm{SDO}_{1}$ holds the lowest $\eta_{E, a v g}$. The $\mathrm{SDO}_{4}$ presented $\eta_{O, \text { avg }}$ over $17 \%$ higher than $\mathrm{SDO}_{1}$, whilst the $\mathrm{SDO}_{2}$ had $\eta_{E, a v g} 1.4 \%$ higher than $\mathrm{SDO}_{1}$.

$$
\begin{align*}
\eta_{O, \text { avg }} & =\frac{\sum_{i=1}^{n_{R T}}\left[\eta_{O} \cdot \delta s\right]_{i}}{\sum_{i=1}^{n_{R}} \delta s_{i}}  \tag{6.1}\\
\eta_{E, \text { avg }} & =\frac{\sum_{i=1}^{n_{R T}}\left[\eta_{E} \cdot \delta s\right]_{i}}{\sum_{i=1}^{n_{R T}} \delta s_{i}} \tag{6.2}
\end{align*}
$$

The $\mathrm{SDO}_{4}$ presents the highest amount of LNG delivered per round trip ( $m_{L N G}$ ) but, in contrast, the lowest annual income because it takes longer to accomplish a round trip $\left(\Delta t_{r n d}\right)$, accomplishing fewer round trips per year $\left(n_{r n d}\right)$. The $\mathrm{SDO}_{1}$ presents the highest income and the lowest CAPEX but, in contrast, the highest OPEX. Thus, these economic measures of merit must be analysed in a combined way, such as performed by NPV. The NPV for the $\mathrm{SDO}_{1}$ is US $\$ 12.3$ million larger than for the $\mathrm{SDO}_{4}$, accounting for a $2.1 \%$ gain. As noted, one of the strengths of the applied optimisation algorithm is achieving a population with various different improved designs, instead of only one. This is important for taking into account last subjective considerations and making the final decision.

### 6.3 Engine and fuel profile effect

Table 6.3 lists average engine efficiency ( $\eta_{E, \text { avg }}$ ), average annual income and OPEX, as well as CAPEX and NPV for every matching of engine configuration and fuel profile (FP) suitable for $\mathrm{SDO}_{2}$. There are five suitable engine configurations and four fuel profiles totalling 20 matchings. In order to facilitate the analysis, the

Table 6.2: Improved synthesis, design and operation (SDO) from the final population.

| Feature | Unit | $\mu$ | $\sigma$ | $\mathrm{SDO}_{1}$ | $\mathrm{SDO}_{2}$ | $\mathrm{SDO}_{3}$ | $\mathrm{SDO}_{4}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $v_{r w, l l}$ | kn | 11.99 | 0.0266 | 12.00 | 12.00 | 12.00 | 11.97 |
| $v_{r w, i l}$ | kn | 15.98 | 0.0262 | 15.97 | 15.99 | 16.00 | 16.00 |
| $v_{r w, h l}$ | kn | 18.04 | 0.4381 | 17.94 | 17.91 | 17.54 | 17.74 |
| $v_{r w, l b}$ | kn | 12.00 | 0.0084 | 12.00 | 12.00 | 12.00 | 12.00 |
| $v_{r w, i b}$ | kn | 15.99 | 0.0175 | 16.00 | 16.00 | 16.00 | 15.97 |
| $v_{r w, h b}$ | kn | 18.41 | 0.4062 | 18.57 | 18.38 | 17.91 | 17.49 |
| $D$ | m | 8.460 | 0.2429 | 8.500 | 8.217 | 8.500 | 8.500 |
| $A_{E} / A_{O}$ | - | 0.7488 | 0.1001 | 0.6460 | 0.7570 | 0.7849 | 0.4196 |
| $P / D$ | - | 0.9277 | 0.0776 | 0.8837 | 1.0195 | 0.9301 | 0.8233 |
| $Z$ | - | 5.0917 | 0.6859 | 5 | 6 | 4 | 3 |
| $Z_{p}$ | - | 1.0333 | 0.1803 | 1 | 1 | 1 | 2 |
| $E_{I D}$ | - | 7.167 | 2.247 | 8 | 7 | 8 | 12 |
| $Z_{c}$ | - | 7.592 | 1.008 | 8 | 7 | 8 | 8 |
| FP | - | 2.000 | 0.000 | 2 | 2 | 2 | 2 |
| $\eta_{O, a v g}$ | $\%$ | - | - | 64.09 | 63.17 | 63.74 | 75.11 |
| $\eta_{E, a v g}$ | $\%$ | - | - | 50.29 | 51.00 | 50.80 | 50.85 |
| $m_{L N G}$ | t | - | - | 70,737 | 70,737 | 70,737 | 70,741 |
| $\Delta t_{r n d}$ | d | - | - | 50.43 | 50.51 | 50.92 | 51.06 |
| $n_{r n d}$ | - | - | - | 7.128 | 7.116 | 7.058 | 7.039 |
| Income | $\mathrm{US} \$ \cdot 10^{6}$ | - | - | 277.7 | 277.2 | 275.0 | 274.3 |
| OPEX | $\mathrm{US} \$ \cdot 10^{6}$ | - | - | 204.8 | 204.5 | 202.6 | 201.8 |
| CAPEX | $\mathrm{US} \$ \cdot 10^{6}$ | - | - | 67.24 | 69.61 | 67.93 | 75.68 |
| NPV | $\mathrm{US} \$ \cdot 10^{6}$ | - | - | 598.3 | 594.8 | 592.8 | 586.0 |

Notes: $\mu$ is average; $\sigma$ is standard deviation; $\mathrm{SDO}_{1}$ is the best (optimum) and $\mathrm{SDO}_{4}$ is the worst.
influence of engine configuration and fuel profile for the $\mathrm{SDO}_{2}$ is also shown as bar charts in Fig. 6.3.

As one may observe, $\eta_{E, \text { avg }}$ is always the highest for $\mathrm{FP}_{4}$ and the lowest for $\mathrm{FP}_{1}$, whereas it is the same intermediate value for $\mathrm{FP}_{2}$ and $\mathrm{FP}_{3}$. This is due to the assumption that engine efficiency depends only on the fuel phase (liquid or gaseous), made in Eq. 5.1 and 5.2 , being independent of the fuel composition. Engine configuration is more influential on CAPEX whereas income and OPEX are more affected by the fuel profile. The $\mathrm{FP}_{I D}$ ranking in descending order of NPV was 2-1-3-4 for every engine. Since the best $\mathrm{FP}_{I D}$ does not occur for the highest efficiency or income, nor for the lowest expenditures, these merit measures analysed individually do not indicate the best project.

Among all five suitable engines, the best alternative regarding NPV was the $4^{\text {th }}$ one: engine 7G70-9.5 ( $E_{I D}=7,7$ cylinders, "green" ultra-long stroke, 700 mm of piston diameter, mark number 9.5), whilst the worst one was the $2^{\text {nd }}$ one: engine 5S90-10.5 ( $E_{I D}=3,5$ cylinders, super long stroke, 900 mm of piston diameter, mark number 10.5). For the best engine, the $\mathrm{FP}_{2}$ led to an increase of US $\$ 22.6$ million on NPV in comparison with the $\mathrm{FP}_{4}$. This means that a simple search for the best fuel profile provided a gain of over $3.9 \%$. Comparing the highest and the worst NPV among all matchings, the gain peaked at US $\$ 29.1$ million, accounting for over $5.1 \%$, which illustrates the combined effect of a simple search for the best matching of engine and fuel profile. Additionally, even for the best engine (7G70-9.5), NPV would be lower than the worst one in Tab. $6.2\left(\mathrm{SDO}_{4}\right)$ if either $\mathrm{FP}_{3}$ or $\mathrm{FP}_{4}$ were chosen.

### 6.4 Weather effect

In order to evaluate the influence of weather conditions, Fig. 6.4 shows the total resistance during laden and ballast trips for rough weather and still water. Weather effect for the laden trip was stronger between way-points 14 and 18 , where the total resistance in rough weather $\left(R_{T, r w}\right)$ was around 139 kN higher than for still water ( $R_{T, s w}$ ), accounting for an increase of over $9.6 \%$. However, the largest total resistance for rough weather occurred in ballast, between way-points 13 and 14, and peaked at 1601 kN . In this case, the added resistance was only 50 kN , representing a $3.2 \%$ increase.

The propeller's open water efficiency was also affected by weather conditions, as shown for the $\mathrm{SDO}_{1}$ in Fig. 6.5. The strongest influence for the laden trip resulted in a decrease of 2.0 percentage points, accounting for under $3.1 \%$, between way-points 14 and 18. For the ballast condition, the effect was most significant between way-points 4 and 5 , where there was a drop of 1.5 percentage points,

Table 6.3: Influence of the matchings of engine configuration and fuel profile for the $\mathrm{SDO}_{2}$

| $E_{I D}$ | Engine | $Z_{c}$ | $\mathrm{FP}_{I D}$ | $\eta_{E, a v g}$ | Income | OPEX | CAPEX | NPV |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | \% | US\$•10 ${ }^{6}$ |  |  |  |
| 2 | G90-10.5 | 5 | 1 | 52.91 | 278.2 | 205.6 | 75.05 | 587.6 |
|  |  |  | 2 | 53.04 | 277.3 | 204.3 | 75.05 | 591.1 |
|  |  |  | 3 | 53.04 | 271.3 | 200.4 | 75.05 | 572.3 |
|  |  |  | 4 | 53.64 | 267.5 | 200.1 | 48.57 | 566.9 |
| 3 | S90-10.5 | 5 | 1 | 52.42 | 278.2 | 205.7 | 76.10 | 586.0 |
|  |  |  | 2 | 52.56 | 277.3 | 204.3 | 76.10 | 589.6 |
|  |  |  | 3 | 52.56 | 271.3 | 200.4 | 76.10 | 570.6 |
|  |  |  | 4 | 53.13 | 267.5 | 200.1 | 49.62 | 565.7 |
| 4 | S90-9.5 | 5 | 1 | 52.05 | 278.2 | 205.7 | 75.90 | 585.9 |
|  |  |  | 2 | 52.21 | 277.3 | 204.4 | 75.90 | 589.6 |
|  |  |  | 3 | 52.21 | 271.2 | 200.4 | 75.90 | 570.5 |
|  |  |  | 4 | 52.80 | 267.5 | 200.1 | 49.42 | 566.0 |
| 7 | G70-9.5 | 7 | 1 | 50.77 | 278.2 | 205.9 | 69.61 | 591.0 |
|  |  |  | 2 | 51.00 | 277.2 | 204.5 | 69.61 | 594.8 |
|  |  |  | 3 | 51.00 | 271.1 | 200.4 | 69.61 | 575.4 |
|  |  |  | 4 | 51.66 | 267.5 | 200.1 | 43.13 | 572.2 |
| 7 | G70-9.5 | 8 | 1 | 51.85 | 278.2 | 205.8 | 73.14 | 588.4 |
|  |  |  | 2 | 52.00 | 277.3 | 204.4 | 73.14 | 592.1 |
|  |  |  | 3 | 52.00 | 271.2 | 200.4 | 73.14 | 573.0 |
|  |  |  | 4 | 52.61 | 267.5 | 200.1 | 46.66 | 568.6 |

Notes: the maximum NPV occurs for the matching 7G70-9.5 and $\mathrm{FP}_{2}$, and the minimum one occurs for $5 \mathrm{~S} 90-10.5$ and $\mathrm{FP}_{4}$.


Figure 6.3: Engine configuration and fuel profile effects for the $\mathrm{SDO}_{2}$.


Figure 6.4: Total resistance throughout the voyage.
accounting for a $2.2 \%$ drop. Moreover, one can see clearly that the propeller's open water efficiency for still water does not present a trend regarding the service speed.


Figure 6.5: Propeller's open water efficiency throughout the voyage for the $\mathrm{SDO}_{1}$.

The required shaft speed throughout the voyage for the $\mathrm{SDO}_{1}$ are shown in Fig. 6.6. The shaft speed for the entire voyage was higher in rough weather $\left(n_{r w}\right)$ than in still water $\left(n_{s w}\right)$. The increase of $n_{r w}$ in laden condition reached 3.9 rpm between way-points 14 and 18 , a $4.8 \%$ increase. However, the highest value of $n_{r w}$ occurred in ballast condition, peaking at about 86 rpm between way-points 13 and 14 , a $3 \%$ increase.

The required brake power throughout the voyage for the $\mathrm{SDO}_{1}$ are shown in Fig. 6.7. The brake power in rough weather $\left(P_{B, r w}\right)$ and laden condition reached


Figure 6.6: Required shaft speed throughout the voyage for the $\mathrm{SDO}_{1}$.
an increase of over 3.9 MW between way-points 14 and 18, an increase of almost $22 \%$ in comparison with still water $\left(P_{B, s w}\right)$. The highest $P_{B, r w}$ occurred, though, in ballast condition, peaking at 23 MW between way-points 13 and 14 , an increase about $13 \%$.


Figure 6.7: Required brake power throughout the voyage for the $\mathrm{SDO}_{1}$.

Owing to the overlap of all those effects, the brake power in rough weather ( $P_{B, r w}$ ) was appreciably increased in comparison to the brake power in still water $\left(P_{B, s w}\right)$. Therefore, the operating point of the engine-propeller matching is primarily affected by the variation in brake power, and secondarily by the variation in shaft speed.

For the purpose of studying the effect of different weathers on the optimisation, June and December 2015 conditions were also considered. June is a milder month
whereas December presents an extremer weather. Table 6.4 lists Beaufort Number (BN) and encounter angle for the laden trip ( $\theta_{l}$ ) along the route-tracks (RT) for June, December and 2015 average. Encounter angle for the ballast trip is the supplementary angle of $\theta_{l}$. More expressive variations in $\theta_{l}$ can be observed whilst BN varies just slightly with respect to its average.

Table 6.4: Varying weather conditions for 2015.

| RT | S [km] | Jun |  | Dec |  | Avg |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | BN | $\theta_{l}\left[{ }^{\circ}\right]$ | BN | $\left.\theta_{l}{ }^{[ }\right]$ | BN | $\theta_{l}\left[^{[ }\right]$ |
| 1-2 | 59.0 | 3 | 15.27 | 4 | 45.66 | 3 | 64.78 |
| 2-3 | 1339 | 3 | 31.01 | 4 | 42.42 | 4 | 47.70 |
| 3-4 | 1339 | 4 | 74.09 | 4 | 83.12 | 4 | 83.55 |
| 4-5 | 77.0 | 2 | 131.4 | 3 | 128.9 | 3 | 132.4 |
| 5-6 | 1015 | 2 | 69.77 | 2 | 98.05 | 3 | 58.33 |
| 6-7 | 1015 | 3 | 142.1 | 3 | 125.2 | 3 | 142.8 |
| 7-8 | 1015 | 3 | 140.5 | 2 | 38.71 | 2 | 42.50 |
| 8-9 | 1015 | 3 | 10.04 | 4 | 59.27 | 3 | 52.42 |
| 9-10 | 1015 | 4 | 30.04 | 4 | 50.95 | 4 | 40.52 |
| 10-11 | 1015 | 4 | 41.17 | 4 | 51.89 | 4 | 48.76 |
| 11-12 | 1015 | 4 | 78.50 | 5 | 17.04 | 4 | 65.82 |
| 12-13 | 1015 | 4 | 88.67 | 6 | 36.56 | 4 | 50.10 |
| 13-14 | 1015 | 4 | 61.06 | 6 | 27.53 | 5 | 36.69 |
| 14-15 | 1015 | 4 | 43.90 | 6 | 12.37 | 5 | 7.438 |
| 15-16 | 1015 | 4 | 20.90 | 6 | 0.055 | 5 | 0.561 |
| 16-17 | 1015 | 4 | 32.11 | 6 | 13.93 | 5 | 12.30 |
| 17-18 | 1015 | 4 | 78.02 | 5 | 31.07 | 5 | 23.21 |
| 18-19 | 1015 | 4 | 93.72 | 5 | 62.08 | 5 | 50.71 |
| 19-20 | 93.0 | 2 | 150.8 | 3 | 42.17 | 3 | 74.54 |

Table 6.5 presents the variable optimal values for weather conditions from June, December and 2015 average. Power and rotational speed for SMCR are presented as well as NPV. The different weather conditions caused some variations on service speed and blade area ratio whilst all the other variables had quite discreet changes. Therefore, the SMCR point and the NPV were slightly affected.

Although more significant influences could be expected, the limited number of engines considered might have forced similar solutions, as shown in Fig. 6.8, As can be seen, the SMCR points are placed on the edge of the $E_{8}$ layout diagram and there are no other engines of larger power for near rotational speeds. Another consideration is that the weather conditions used were approximated from monthly means of daily means. Hence, the occasional most severe weather conditions were balanced by milder conditions, affecting insignificantly the mean. That is why the three conditions assessed are not so different.

Table 6.5: Optimal synthesis, design and operation for varying adverse weather conditions.

| Feature | Unit | Jun | Dec | Avg |
| :---: | :---: | :---: | :---: | :---: |
| $v_{r w, l l}$ | kn | 12.00 | 12.00 | 12.00 |
| $v_{r w, i l}$ | kn | 16.00 | 15.95 | 15.97 |
| $v_{r w, h l}$ | kn | 18.14 | 17.91 | 17.94 |
| $v_{r w, l b}$ | kn | 12.00 | 12.00 | 12.00 |
| $v_{r w, i b}$ | kn | 16.00 | 15.92 | 16.00 |
| $v_{r w, h b}$ | kn | 18.64 | 18.52 | 18.57 |
| $D$ | m | 8.424 | 8.500 | 8.500 |
| $A_{E} / A_{O}$ | - | 0.6863 | 0.7533 | 0.6460 |
| $P / D$ | - | 0.8803 | 0.8788 | 0.8837 |
| $Z$ | - | 5 | 5 | 5 |
| $Z_{p}$ | - | 1 | 1 | 1 |
| $E_{I D}$ | - | 8 | 8 | 8 |
| $Z_{c}$ | - | 8 | 8 | 8 |
| $F P_{I D}$ | - | 2 | 2 | 2 |
| $P_{S M C R}$ | MW | 25.60 | 25.60 | 25.52 |
| $n_{S M C R}$ | rpm | 90.92 | 89.78 | 89.22 |
| NPV | $\mathrm{US} \$ \cdot 10^{6}$ | 600.4 | 596.3 | 598.3 |



Figure 6.8: SMCR points for weather conditions from different months.

### 6.5 Economic scene effect

There is a strong relationship between the optimum fuel profile and the fuel and LNG prices, as previously mentioned. In order to assess the influence of different economic scenes on the optimum synthesis, design and operation, a data collection about fuels and LNG prices were carried out. Figure 6.9 shows the annual average prices of fuels and LNG for the period between 2000 and 2015, as well as the averages for this entire interval. Although there are appreciable alterations every year, the global average MGO price ( $c_{M G O, \text { avg }}$ ) is almost coincident with the average LNG cost, insurance and freight $\left(C I F_{L N G, a v g}\right)$. Likewise, the global average HFO price $\left(c_{H F O, a v g}\right)$ is almost coincident with the average LNG free on board ( $F O B_{L N G, a v g}$ ).


Figure 6.9: Fluctuation in fuel and LNG prices.

Table 6.6 shows five economic scenes and the global average (Avg). These scenes were selected as they are completely distinct from one another, being quite influential on the optimisation. Therefore, the optimisation process was run for each one of the economic scenes whilst the other input data were kept as stated in Chap. 5. Figure 6.10 illustrates the evolution of the optimisation variables along the generations whilst Tab. 6.7 lists the optimal synthesis, design and operation variables, as well as the NPV, for those selected economic scenes.

The optimisation variables were seen to evolute differently along the generations for each economic scene in Fig. 6.10. The optimal configurations were also different, evidencing the influence of the economic scene on the synthesis, design and operation of the system. As previously noticed, the best configuration presents a steady value of fuel profile $\left(F P_{I D}\right)$ along the generations, independently of the economic scene.

Table 6.6: Selected economic scenes.

| Year | $c_{H F O}[\mathrm{US} \$ / \mathrm{t}]$ | $c_{M G O}[\mathrm{US} \$ / \mathrm{t}]$ | $C I F_{L N G}[\mathrm{US} \$ / \mathrm{t}]$ | $F O B_{L N G}[\mathrm{US} \$ / \mathrm{t}]$ |
| :---: | :---: | :---: | :---: | :---: |
| 2003 | 193.6 | 287.7 | 557.7 | 391.0 |
| 2006 | 411.3 | 655.0 | 796.7 | 522.5 |
| 2008 | 620.7 | 914.7 | 812.0 | 640.7 |
| 2012 | 585.7 | 976.8 | 537.8 | 257.6 |
| 2015 | 303.0 | 522.2 | 525.2 | 260.9 |
| Avg | 397.0 | 615.6 | 613.4 | 389.7 |

However, the optimum $F P_{I D}$ was $F P_{1}$ for the 2003 scene; $F P_{2}$ for the 2006, 2008, 2015 and average scene; and $F P_{4}$ for the 2012 scene. The $F P_{3}$, though, was not the optimum for any of the selected economic scenes.

Remembering the description of the fuel profiles (Sec. 5.3), it is acceptable to assume that the $F P_{1}$ was the optimum only for the 2003 scene as it was the only time that $c_{H F O}$ and $c_{M G O}$ were both lower than $F O B_{L N G}$. In this case, it is more advantageous to burn HFO and MGO, and to sell all the LNG cargo. The $F P_{4}$ was the optimum only for the 2012 scene as it was the only time that $F O B_{L N G}$ and $C I F_{L N G}$ were both lower than $c_{H F O}$. In this case, the income from the LNG supposedly sold, instead of burnt, would not compensate for the cost of HFO theoretically used. For the years 2006 and 2008, the use of HFO instead of BOG is predictable because $c_{H F O}$ is lower than $F O B_{L N G}$. The same does not occur in 2015 and in the average scene, in which, although $c_{H F O}$ is between $F O B_{L N G}$ and $C I F_{L N G}, F P_{2}$ was the best one. In this case, the use of BOG as fuel would decrease OPEX but it would also decrease incomes more sharply.

As can be seen in Tab. 6.7, the various economic scenes provided quite different configurations with expressive variations on NPV. The high service speeds varied either in laden or ballast ( $v_{r w, h l}$ or $v_{r w, h b}$ ) whilst the most of the others remained steady. In five out of the six cases, the diameter of the propeller was its only parameter converging to the same value. The different diameter coincided with the only variation in the number of propulsion chains $\left(Z_{p}\right)$. The NPV for 2012 scene and $F P_{4}$ was $36 \%$ higher than for the average ( Avg ) scene and $F P_{2}$. Furthermore, a remarkable difference of over $120 \%$ was found by comparing the NPV for the 2012 scene and $F P_{4}$ with the 2008 scene and $F P_{2}$, highlighting the influence of the economic scene and fuel profile on the synthesis, design and operation of the system.

### 6.6 Strengths of the approach

A list summarising the main strengths of the approach may be found below.

+ The total processing time to run all the cases presented herein was under 52


Figure 6.10: Evolution of the optimisation variables for the selected economic scenes.

Table 6.7: Optimal synthesis, design and operation for the selected economic scenes.

| Feature | Unit | 2003 | 2006 | 2008 | 2012 | 2015 | Avg |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $v_{r w, l l}$ | kn | 11.95 | 12.00 | 12.00 | 12.00 | 12.00 | 12.00 |
| $v_{r w, i l}$ | kn | 15.98 | 16.00 | 16.00 | 16.00 | 16.00 | 16.00 |
| $v_{r w, h l}$ | kn | 17.86 | 19.50 | 16.62 | 19.50 | 19.03 | 18.01 |
| $v_{r w, l b}$ | kn | 12.00 | 12.00 | 12.00 | 12.00 | 12.00 | 12.00 |
| $v_{r w, i b}$ | kn | 16.00 | 16.00 | 16.00 | 16.00 | 15.97 | 16.00 |
| $v_{r w, h b}$ | kn | 18.47 | 19.50 | 17.12 | 19.50 | 19.50 | 18.52 |
| $D$ | m | 8.500 | 8.500 | 8.500 | 8.500 | 7.648 | 8.500 |
| $A_{E} / A_{O}$ | - | 0.6561 | 0.8238 | 0.5128 | 0.8208 | 0.4702 | 0.7158 |
| $P / D$ | - | 0.8969 | 1.0751 | 0.8037 | 1.0924 | 0.9070 | 0.8958 |
| $Z$ | - | 5 | 6 | 3 | 6 | 3 | 5 |
| $Z_{p}$ | - | 1 | 1 | 1 | 1 | 2 | 1 |
| $E_{I D}$ | - | 8 | 2 | 10 | 2 | 12 | 8 |
| $Z_{c}$ | - | 8 | 6 | 8 | 6 | 9 | 8 |
| $\mathrm{FP}_{I D}$ | - | 1 | 2 | 2 | 4 | 2 | 2 |
| NPV | $\mathrm{US} \$ \cdot 10^{6}$ | 573.8 | 1011.5 | 483.3 | 1065.6 | 1001.4 | 783.7 |

hours, thereby the approach can be considered fast enough for an early-stage optimisation.

+ Technical constraints were taken into account to avoid propeller configurations that might present problems related to strength, cavitation, vibration and noise.
+ The approach searches for the best engine-propeller matching amongst all the technical possibilities.
+ Different sea conditions can be considered for each route-track and the weather conditions required by the Kwon's added resistance method are only Beaufort Number and encounter angle.
+ Different parameters can be set up in each route-track and this enables various operational profiles to be considered to seek the highest net present value.


### 6.7 Limitations of the approach

Since an early-stage design optimisation approach must be fast, only simpler models were used. However, the simpler, the more limited they are. Each one of the models has its own limitations that, in turn, become limitations of the overall approach. Thus, the main limitations of the approach, besides those, are listed following.

- The influences of the water depth were not considered at all, such that the service margin component due to water depth was based on deep water. Therewith, the approach is inappropriate for shallow water.
- Appendages were neglected in the resistance calculation that considers merely form parameters, not the hull design itself.
- Neither a waste heat recovery system nor a gas after-treatment equipment was incorporated in the approach. Likewise, a re-liquefaction plant was not modelled and thereby the BOG properties were considered constant as well as its evaporation rate.
- Noxious emissions were considered neither to constraint the service speed nor to include additional fees. Similarly, no design index were considered either as a constraint or an additional objective function.
- A constant weather condition along the ship's life-cycle is a simplifying hypothesis. Severe sea conditions might cause overload on the engine and propeller, as well as might cause cavitation increase, which affects the behaviour of the propeller. The propeller might even emerge from the water and the engine might not be able to keep the ship service speed. Those situations were not taken into account.
- The Kwon's model does not consider wave amplitude, wavelength or frequency, such that if a more detailed model were used, the reliability of the approach could increase.


## Chapter 7

## Conclusion

This work has proposed a comprehensive early-stage approach to perform the optimisation of synthesis, design and operation for an LNGC under rough weather. Since an engine model suitable for optimisation problems was not found, developing such a model has been the first step of this work. It has been considered fixed pitch propellers directly driven by dual-fuel low-speed Diesel engines. Constraints have been incorporated to the approach in order to avoid propellers that could present issues concerning strength, cavitation and vibration. Different fuel profiles and service speeds have also been assessed. The approach proposed herein has used a differential evolution optimisation algorithm to optimise fourteen parameters. The objective function to be maximised by the algorithm has been the net present value for the ship's lifetime.

The computation of 15,023 input data sets have been run in 5.9 hours and almost $48 \%$ of the configurations have been constrained, the peripheral velocity being responsible for most rejections. The worst individual of the final population has had the objective function increased by $22 \%$ in comparison to the worst individual of the initial population. The final population has included rather distinct designs with a variation of only $2.1 \%$ in the objective function, which is a strength of the approach. Thus, subjective considerations may be taken into account before the final decision with only minor concerns.

Analysing the rejected configurations and why they have been rejected, there have not been general recommendations about configuration so that the propellers could escape the constraints. The best design has not held the most efficient either propeller or engine but the highest OPEX, which emphasises that these measures of merit must not be considered separately. An appropriate objective function must consider them in combination, such as done by the net present value. A simple search for the best matching of fuel profile and engine has provided a gain of over 5.1\%.

The average weather condition for 2015 have led to almost $22 \%$ increase in brake
power and $4.8 \%$ increase in shaft speed, emphasizing the effect on the engine and propeller operating points. On the other hand, the assessment of weather conditions from different months in 2015 did not show significant effects. One reason for this was the limited number of engines considered that forced the convergence to similar SMCR points. Another reason is that the weather conditions used were approximated from monthly means of daily means, being not so different one another.

The optimisation variables were seen to evolute differently along the generations for each one of the six economic scenes studied. The optimal configurations were also affected. It was seen that the use of BOG as fuel would decrease OPEX but it would also decrease incomes more sharply, depending on the economic scene. A remarkable difference of over $120 \%$ was found by comparing the NPV for the best economic scene with the worst one. Thus, the combined influence of economic scene and fuel profile on the synthesis, design and operation of the system was underlined.

Ultimately, the approach has shown significant gains and highlighted the need for exploring a broad range of propellers and engines, as well as considering the weather conditions in an integrated way. Assessing various profiles of fuel and service speed, as well as different economic scenes, was shown meaningful to found the configuration that maximises the NPV. Although an LNGC has been considered, this approach could be applied to other types of ships with only minor adjustments.

## Chapter 8

## Written articles and future work

This chapter sums up the articles written during the doctoral period and gives some possible courses of action to seek improvements in the developed approach.

### 8.1 Written articles

Some articles have been written and submitted to congresses and journals during the doctoral period. All of them are listed and their publication is briefly described below. Besides, the first page of each article is attached as appendix.

1. Literature review of an LNG carrier machinery system (Sec. A.1) - this paper was presented at the $16^{\text {th }}$ International Congress of the International Maritime Association of the Mediterranean (IMAM 2015), from 21 to 24 September 2015, in Pula, Croatia, and then it was published as a chapter in the book Towards Green Marine Technology and Transport.
2. Optimised selection of marine dual-fuel low-speed Diesel engines: introducing relative specific fuel consumptions (Sec. A.2) - this paper was submitted to the journal Marine Systems \& Ocean Technology on 14 March 2016 and accepted on 7 September 2016.
3. A model to optimise the selection of marine dual-fuel low-speed Diesel engines (Sec. A.3) - this paper was presented at the $26^{\text {th }}$ National Congress on Maritime Transportation, Ship and Offshore Construction (SOBENA 2016), from 8 to 10 November 2016, in Rio de Janeiro, Brazil. Afterwards, the paper was encouraged to be sent to the journal Marine Systems \& Ocean Technology, being submitted on 29 November 2016 and accepted on 30 May 2017.
4. An approach to optimise the selection of LNG carriers' propulsion system (Sec. A.4) - this paper was presented at the VII Seminar and Workshop
in Ocean Engineering (SEMENGO 2016), from 23 to 25 November 2016, in Rio Grande, Brazil. Afterwards, the paper was encouraged to be sent to the journal Thermal Engineering (RETERM), being submitted on 11 May 2017 and accepted on 6 July 2017.
5. Matching engine to propeller for an LNGC under rough weather (Sec. A.5) this paper was presented at the $17^{\text {th }}$ International Congress of the International Maritime Association of the Mediterranean (IMAM 2017), from 9 to 11 October 2017, in Lisbon, Portugal. The paper is likely to become a chapter in the book Maritime Transportation and Harvesting of Sea Resources, which is expected to be published in 2018.
6. Optimising the engine-propeller matching for a liquefied natural gas carrier under rough weather (Sec. A.6) - this paper was submitted to the journal Applied Energy on 13 July 2017 but is still under review.

### 8.2 Future work

Only articles addressing partially the approach developed and the results found herein have been written so far. Hence, the first future work to be performed is a paper covering entirely the approach and results. Afterwards, the following list of future works can be performed in any order.

- Since different input data have not been simulated, the sensitivity of the net present value to input data, as ship and energy system parameters for instance, may be studied. Thus, ships of various geometries and cargo capacities can be assessed in order to find out which one holds the highest net present value. Furthermore, the ship's geometric parameters can be taken as design variables. In this case, a relation between cargo capacity and geometry would be need so that the best geometry could be found.
- Various routes could be studied in order to find the one maximising the NPV. The optimum design, synthesis and operation of the ship energy system depend on the weather condition of each route. Therefore, perhaps lengthier routes whose weather is less rough provide higher NPV than the shortest route (great circle route).
- As the best parameter values of the optimisation algorithm depend on every single problem, they could be optimised to enhance the algorithm performance. Moreover, other stochastic optimisation algorithms, such as simulated annealing and particle swarm, for instance, could be adopted. Thus,
their performances could be compared to each other to figure out the best algorithm to use in this case.
- If fuel and LNG prices, as well as weather conditions, follow typical patterns, they could be explained by deterministic functions. However, these parameters are also influenced by uncertain factors, which are the drivers of stochastic components. Hence, the simulation of these parameters should take into account both deterministic and stochastic components. In future works, they may be considered as probability distributions or treated by models as the geometric Brownian motion or mean-reversion model. In this sense, the robustness of solution is a substantial measure that was not treated in the present study. The degree of robustness to be supplied for a satisfactory solution is related to the system variations most likely to occur.
- Since the weather condition, as well as the fuel and LNG prices, are time-dependent parameters, the problem could be modelled as a dynamic optimisation problem (DOP). The goal of methods dealing with DOPs is no longer to locate a stationary optimal solution but to track its movement through the solution and time spaces as close as possible. Evolutionary techniques and their variants have been the most widely used methods to solve DOPs, but other approaches are gaining ever more attention in the past years [66].


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## Appendix A

## Linked articles

Next, it is attached the first page of each article written along the doctoral period. All have been published, except the last article A.6), which is still under review.

# A. 1 First article 

# Literature review of a LNG carrier machinery system 

C.R.P. Belchior<br>Department of Oceanic and Naval Engineering, Federal University of Rio de Janeiro, Rio de Janeiro, Brazil<br>C.H. Marques<br>School of Engineering, Federal University of Rio Grande, Rio Grande do Sul, Brazil


#### Abstract

The present study aims to inform about some important subjects to take into account when it is beginning to work with liquefied natural gas carrier machinery systems. Firstly, some general information about liquefied natural gas and ships that carry it were presented. Then, reasons why the traditional steam turbine propulsion plant was abandoned, as well as alternative propulsion plants were addressed. Two-stroke slow speed diesel engines without reliquefaction plant, as well as dual-fuel diesel electric and dual-fuel direct drive propulsion plants were discussed. Further, basic knowledge about reliquefaction plant was presented and a way to evaluate its viability was explained. Taking into account the environmental concern, some alternatives for ballast operation and some issues about gaseous emissions were discussed, as well as manners to reduce these emissions were addressed. Lastly, options to increase the overall propulsion plant efficiency using the exhaust gas waste heat were presented.


## 1 INTRODUCTION

LNG carriers are specialized ships designed to transport Liquefied Natural Gas (LNG).They are fitted with insulated double-hulled tanks, designed to contain the cargo slightly above atmospheric pressure at a cryogenic temperature of approximately $-169^{\circ} \mathrm{C}$. An average LNG carrier presents tank capacity about $160,000 \mathrm{~m}^{3}$ and typically, the storage tanks operate at $0.3 \mathrm{bar}_{\mathrm{g}}$ with a design pressure of 0.7 bar $_{\mathrm{g}}$. LNG presents typically density between 430 and $470 \mathrm{~kg} / \mathrm{m}^{3}$, depending on its composition and state. The LNG is composed predominantly by methane $\left(\mathrm{CH}_{4}\right)$, as well as ethane $\left(\mathrm{C}_{2} \mathrm{H}_{6}\right)$, propane $\left(\mathrm{C}_{3} \mathrm{H}_{8}\right)$, butane $\left(\mathrm{C}_{4} \mathrm{H}_{10}\right)$ and nitrogen ( $\mathrm{N}_{2}$ ). (Mokhatab et al. 2014)

Despite the high degree of insulation in the tank walls, it is impossible to avoid the heat transfer from the surroundings, so that some vaporization will be always present during LNG transportation by ships. This occurs mainly due the thermal conductivity through the tank walls and the movement of the liquid. That LNG evaporated is called Boil-off Gas (BOG) and its evaporation rate is called Boil-off Rate (BOR). The natural BOR from a typical LNG carrier tank is about 0.10 to $0.15 \%$ in volume per day, depending on the thermal insulation system (Mokhatab et al. 2014). Vaporization induces an increase in pressure in the tank, such that a certain amount of the vapour phase should be taken out of the tank to avoid dangerous overpressure. Usually, this outlet gas flow is used as fuel
by the propulsion system of the ship to reduce its fuel consumption. (Miana et al. 2010)

One of the major advantages of using steam propulsion plant in LNG carriers has been its capability to burn the unavoidable BOG directly in the power boiler, which has made it practically an exclusive option for many years. However, as environmental, economic and technical expectations have increased, the drawbacks of the steam turbine power plant have made it a less attractive option. Among these drawbacks are the comparative low efficiency of the plant, its high fuel consumption, which in turn translates into high exhaust emissions and its large engine room space requirement. Advances in the design of dualfuel diesel engines, shipboard LNG reliquefaction plants and marine gas turbines, provide meaningful alternatives to the traditional steam power plant for LNG vessels. (Gilmore et al. 2005)

Regarding to environmental concern, controls on exhaust gas emissions continue to tighten regionally and internationally dictating further responses from engine designers. Carbon dioxide (CO2), nitrogen oxides $\left(\mathrm{NO}_{\mathrm{x}}\right)$, sulphur oxides $\left(\mathrm{SO}_{\mathrm{x}}\right)$ and Particulate Materials (PM) are the gaseous emissions of most concern. Thereby, in-engine measures to decrease these emissions, including common rail fuel systems, emulsified fuel, direct water injection and charge air humidification, have been studied. In addition, exhaust gas aftertreatment, such as Selective Catalytic Reduction (SCR) and Exhaust Gas Recirculation (EGR)

## A. 2 Second article

# Optimised selection of marine dual-fuel low-speed diesel engines: introducing relative specific fuel consumptions 

Crístofer H. Marques ${ }^{1,2}$ (1) Carlos R. P. Belchior ${ }^{2}$

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#### Abstract

Low-speed diesel engines are the most used ones in large ships as main propulsion, and due to severe environmental rules, there has been an intensive search for using alternative fuels which generate less emissions in these engines. In this context, dual-fuel diesel engines have been developed and their employment keeps growing. Therefore, the present study aimed to elaborate a simple and fast approach to assist the selection of the optimal marine dual-fuel low-speed diesel engine concerning fuel consumption to be fitted as primary mover. Relative specific fuel consumptions were introduced to develop unified expressions, and a polynomial approach was applied in order to fit curves. The accuracy of the method was verified through comparisons with a web-based application provided by an engine manufacturer and the highest deviation peaked at about $2.7 \%$. A practical liquefied natural gas carrier design of matching propeller/ship and engine was performed so that the convenience of the method could be explored. Thus, through the proposed optimisation methodology, annual savings of over 8.1 and $9.6 \%$ were reached regarding heavy fuel oil and boil-off gas, respectively. At last, it was found that the optimal matching might not be due to the most efficient either propeller or engine.


[^8]Keywords Optimisation • Selection • Dual-fuel diesel engine • Low-speed diesel engine • Marine propulsion • Prime mover

## 1 Introduction

Prime mover selection is one of the major steps in merchant ship building projects. Since this machine is usually operated until the end of the ship's lifetime, its selection is made taking into account its durability. The importance of each selection criteria differs from one to another ship type. In some ships, only a few of the criteria need to be considered, in others all must be taken into account although with different degrees of emphasis. The most applied prime mover in merchant transportation of large scale has been the low-speed diesel engine, and factors influencing its selection can be classified into two categories: technical aspects and financial aspects. Noise, vibration, emissions, size, weight and efficiency are only some examples of the former whilst capital expenditures and operational expenditures summarise the latter.

Criteria designation is a highly difficult problem due to the fact that many products are not provided with detailed information about their performance and particulars. On the other hand, some indicators may provide information about the engine's performance, such as, time used in the existing fleet, previous damage records, and so forth. Although a complete criteria list for choosing main machinery are given by Watson [1] and many considerations are done by Lamb [2], Bulut et al. [3] based on interviews with a group of technical experts and managers of selected shipping companies defined the following six major selection criteria: power, acquisition cost, fuel

## A. 3 Third article

# A model to optimise the selection of marine dual-fuel low-speed diesel engines 

Crístofer Hood Marques ${ }^{1,2}$ (0) Carlos Rodrigues Pereira Belchior ${ }^{2}$ Jean David Job Emmanuel Marie Caprace ${ }^{2}$

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#### Abstract

This study aimed to address the state of the art of marine diesel engines computer simulation models and the main computer applications. There are simple models based on transfer function or more complex models based on computational fluid dynamics. The models may be either implemented through basic programming languages or simulated through dedicated packages of internal combustion engine simulation. Owing to the recent interest to reduce the gas emission, dual-fuel engines are increasingly being used as primary propulsion in merchant ships. In this context, a simplified model of marine dual-fuel low-speed diesel engine has been developed. Through the normalisation of specific fuel consumption and exhaust gas data, clear trends approachable by polynomial curves or surfaces were revealed. Thus, by using the proposed model and knowing the characteristics of an engine at its nominal maximum continuous rating, it is possible to predict the engine operation in any design point on the engine layout diagram, even at part load. The maximum deviations regarding the two simulated engines did not exceed $-3.4 \%$. Summarising, the developed model is a simple and effective tool for optimising the selection of dual-fuel lowspeed diesel engines to be applied in ship propulsion systems.


Keywords Marine propulsion • Prime mover Optimisation • Prediction model • Selection

[^9]
## 1 Introduction

The earliest engine models were based on ideal (air standard) cycles [1] and are currently the most widely taught in undergraduate courses. Although these were very simplistic, they helped the engineers to understand engine operation. The first of these models is supposed to have been developed in the late 1800s [2]

On the other hand, internal combustion engine simulations itself have been developed and applied since the 1960s. It consists in reproducing mathematically the significant processes and predicting the performance and operation details. In the beginning, the simulations were fairly elementary and limited by both computing capabilities and a lack of knowledge concerning some key submodels. Nowadays, many of these simulations contain advanced and detailed sub-models about fluid mechanics, heat transfer, friction, combustion and chemical kinetics, being performed by sophisticated computer programs [3].

The earliest works on compression ignition engines are perhaps due to McAulay et al. [4], as well as Krieger and Borman [5]. Their simulations were fairly complete, but a major weakness was the lack of a comprehensive description of the complex diesel engine combustion process.

The development of engine cycle simulations is a challenging task largely because of turbulent and unsteady flow, non-uniform mixture composition, highly exothermic chemical reactions, two or three phase compositions, as well as pollutant species. In addition, the important time scales have a large dynamic range of between $1 \mu \mathrm{~s}$ and 1 s , and the important length scales range roughly between $1 \mu \mathrm{~m}$ and 1 m

According to Schulten [6], five main sorts of engine model might be recognised: computational fluid dynamics

## A. 4 Fourth article

## Tecnologia/Technology

# AN APPROACH TO OPTIMISE THE SELECTION OF LNG CARRIERS' PROPULSION SYSTEM 

## C. H. Marques ${ }^{\text {a }}$ <br> C. R. P. Belchior ${ }^{\text {b }}$,

and J. -D. Caprace ${ }^{\text {b }}$

Universidade Federal do Rio Grande
Escola de Engenharia
Avenida Itália, km 8, CP. 474
Rio Grande, RS, Brasil
cristoferhood@oceanica.ufrj.br
${ }^{\mathrm{b}}$ Universidade Federal do Rio de Janeiro
Departamento de Engenharia Naval e Oceânica
Avenida Horácio Macedo, 2030, CP. 68508
Ilha do Fundão, Rio de Janeiro, RJ, Brasil

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#### Abstract

Marine transport of natural gas, mostly in its liquid phase, is of growing importance in the global energy markets. The fleet of liquefied natural gas carriers is thereby increasing and being upgraded to enhance its performance. Since there is no well-defined procedure about how to perform the selection of the propulsion system considering the peculiarities of this kind of vessel, this work intend to fill this gap. In other words, the present article aims to propose an approach so that one can perform the optimised selection of liquefied natural gas carriers' propulsion system mainly concerning financial aspects. Firstly, some fundamentals about liquefied natural gas and its transport are presented followed by reasons why the traditional steam turbine propulsion plant was abandoned and dualfuel diesel engines have been applied instead. Then, a list of criteria is discussed and studies that inspired this work are summarised. A case study of a ship with cargo capacity of $174,000 \mathrm{~m}^{3}$ operating between Lake Charles and Tokyo Bay via Panama Canal is selected. Owing to this route and environmental rules, the ship has to travel at three different levels of service speed unlike ordinary ones, which usually keep a steady speed throughout voyage. Maximising the net present value of the project is the objective function that is intended to be achieved by optimising eleven variables regarding synthesis, design and operation of the propulsion system. Finally, it is suggested that this work may assist marine engineers and ship-owners to design and outline the operation of liquefied natural gas carriers.

Keywords: propulsion, dual-fuel engine, prime mover, optimisation, LNG


| NOMENCLATURE |  |
| :--- | :--- |
|  |  |
| $1+k_{I}$ | form factor of the hull, N |
| $A_{E} / A_{O}$ | blade-area ratio |
| $C_{f o r m}$ | ship form coefficient |
| $C_{n}$ | coefficients of the Troost series polynomials |
| $C_{U}$ | speed reduction coefficient |
| $C_{\beta}$ | direction reduction coefficient |
| $D$ | propeller diameter, m |
| $F$ | net cash flow, US\$ |
| $i$ | discount rate |
| $J$ | advance ratio |
| $K_{Q}$ | non-dimensional torque coefficient |
| $K_{T}$ | non-dimensional thrust coefficients |
| $n$ | number of terms in Troost series polynomials |
| $n_{e}$ | engine speed, rpm |
| $P / D$ | pitch ratio |
| $P_{B}$ | brake power, W |
| $P_{E}$ | effective power, W |
| $R_{A}$ | model-ship correlation resistance, N |
| $R_{A P P}$ | appendage resistance, N |
| $R_{B}$ | additional pressure resistance of bulbous bow |
| $R_{F}$ | near the water surface, N |
| $R_{T}$ | frictional resistance, N |
| $R_{T R}$ | additional resistance, N |
| $R_{W}$ | immersion, N |
| $s_{n}$ | wave resistance, N |
| $t$ | exponents of $J$ (Troost series polynomials) |
| $t_{n}$ | exponents of $P / D$ (Troost series polynomials) |

time of cash flow, year
$Z \quad$ blade number of the propeller
$Z_{c} \quad$ number of cylinders
$Z_{p} \quad$ number of propellers and engines
$\eta_{H} \quad$ hull efficiency
$\eta_{O} \quad$ open water propeller efficiency
$\eta_{R} \quad$ relative rotative efficiency
$\eta_{\text {TRM }}$ transmission efficiency

## Subscripts

$r$ normalised in relation to nominal maximum continuous rating

## Abbreviations

BOG boil-off gas
BOR boil-off rate
CAPEX capital expenditure, US\$
EM engine margin
FP fuel profile
GCU gas combustion unit
HFO heavy fuel oil
ID engine identification
ITTC International Towing Tank Conference

## A. 5 Fifth article

# Matching engine to propeller for an LNGC under rough weather 

C.H. Marques<br>Engineering School, Federal University of Rio Grande (FURG), Rio Grande, Brazil Currently at UFRJ<br>C.R.P. Belchior \& J.-D. Caprace<br>Department of Marine and Ocean Engineering, Federal University of Rio de Janeiro (UFRJ), Rio de Janeiro, Brazil


#### Abstract

The present work aims to provide a comprehensive approach to perform the engine to propeller matching for a Liquefied Natural Gas Carrier (LNGC) under rough weather. A weather condition was included in the assessment of total resistance, and thereby affected the propeller's open water efficiency, shaft speed and brake power. Constraints were included to the approach in order to avoid propellers that could present issues concerning strength, cavitation and vibration. The case study was designed using an LNGC of $175,000 \mathrm{~m}^{3}$ holding three service speeds. Thus, the propeller to engine matchings were addressed for 10 randomly chosen propulsion installations. The lowest total required power was over $14 \%$ lower than the highest. Brake power for rough weather was over $18 \%$ higher than for still water. Therefore, the approach proved useful and highlighted the need to explore a broad range of propellers and engines, as well as to consider weather conditions.


## 1 INTRODUCTION

Liquefied natural gas carriers (LNGCs) are specialised ships designed to transport liquefied natural gas. They are fitted with insulated doublehulled tanks, designed to contain the cargo slightly above atmospheric pressure at a cryogenic temperature without any means of external refrigeration. Despite the high degree of insulation, some vapourisation will occur due to the unavoidable heat transfer from the surroundings to the cargo. Since vapourisation induces a pressure increase in the tank, a certain amount of the vapour phase should be taken out of the tank to avoid dangerous overpressure (Mokhatab et al. 2014). Usually, this outlet gas flow is used as fuel by the marine energy system of the ship to reduce its main fuel consumption (Miana et al. 2010).

For many years steam propulsion plants were practically an exclusive option for LNGCs due to its capability to burn the unavoidable boil-off gas (BOG) directly in the power boiler. However, advances in the design of dual-fuel diesel engines, shipboard BOGre-liquefaction plants and marine gas turbines have provided meaningful alternatives to the traditional steam power plant (Belchior and Marques 2015). Moreover, propulsion systems based on slow speed two-stroke diesel engines driving fixed pitch propellerswith onboard re-liquefaction system have been successfully used in large LNGCs. However, when
conventional fuel prices are higher than LNG price, the operational expenditure of propulsion systems that are unable to use BOG as fuel is increased (Mokhatab et al. 2014). Moreover, conventional fuels are not as clean as BOG, once natural gas is considered environmentally friendly (Kumar et al. 2011). An option to overcome these drawbacks is to apply dual-fuel diesel engines, which are compression ignition ones capable to work in two operational modes: diesel mode and gas mode. During diesel mode they work as a conventional diesel engine, burning ordinary liquid fuels such as marine gas oil, marine diesel oil and heavy fuel oil. In gas mode they burn essentially a gaseous fuel and only a little fraction of liquid pilot fuel is required to start the combustion process (Woodyard 2009).

Since the prime mover is usually operated until the end of the ships lifetime, its selection is one of the major steps in merchant shipbuilding projects. Based on interviews with a group of technical experts and managers of selected shipping companies, Bulut et al. (2015) placed power on the top of the selection criteria list. This is because the engine needs to be capable to provide enough power to satisfy the ships operational profile. Since the propulsion power required by the ship depends on the weather conditions, it is advisable to apply an approach that considers the added resistance due to weather to perform the appropriate selection of the prime mover.

# A. 6 Sixth article 

Manuscript Number: APEN-D-17-05771

Title: Optimising the engine-propeller matching for a liquefied natural gas carrier under rough weather

Article Type: Research Paper
Keywords: optimisation; propulsion; dual-fuel diesel engine; fixed pitch propeller; fuel consumption

Corresponding Author: Mr. Crístofer Hood Marques, Sc.M
Corresponding Author's Institution: FURG
First Author: Crístofer Hood Marques, Sc.M
Order of Authors: Crístofer Hood Marques, Sc.M; Carlos Rodrigues P Belchior, Sc.D; Jean David J Caprace, Ph.D

Abstract: Dual-fuel diesel engines have become the most interesting alternative for liquefied natural gas carriers (LNGCs), since they are able to use boil-off gas (BOG) as fuel. However, there is a lack of studies about the optimisation of propulsion system selection considering weather conditions in an integrated approach. Thus, the present work aims to provide a comprehensive approach to perform the optimisation of engine-propeller matching for an LNGC under rough weather. A weather condition was included in the assessment of total resistance, and thereby affected the propeller's open water efficiency, shaft speed and brake power. Constraints were included to the approach in order to avoid propellers that could present issues concerning strength, cavitation and vibration. A differential evolution optimisation algorithm was applied in which the objective function minimises fuel expenditure for propulsion for a round trip. The case study was designed using an LNGC with a cargo capacity of $175,000 \mathrm{~m}^{3}$ sailing in laden condition from Lake Charles (USA) to Tokyo Bay (Japan), via Panama Canal, and returning in ballast. All suitable matchings for 5346 propellers were found in 2.8 hours and over $28 \%$ of them were constrained. The method has shown a gain of $19 \%$ between the worst individual of the initial population and the worst individual of the final population. The required brake power was approximately $20 \%$ higher for rough weather than for still water. Therefore, the approach used here has shown a significant gain and highlighted the value of exploring a broad range of propellers and engines in an integrated manner, as well as considering the weather condition.


[^0]:    ${ }^{1}$ Gauge pressure

[^1]:    ${ }^{1}$ Gas injection methane
    ${ }^{2}$ Electronically controlled

[^2]:    ${ }^{3}$ Subscripts max and min stand respectively for maximum and minimum
    ${ }^{4}$ Absolute pressure

[^3]:    ${ }^{5}$ Subscript $N$ stands for normalised with respect to NMCR

[^4]:    ${ }^{6}$ Subscript $S$ stands for normalised with respect to SMCR

[^5]:    ${ }^{7}$ Subscript $g$ stands for gas mode

[^6]:    ${ }^{8}$ Subscript $e$ stands for error

[^7]:    ${ }^{1}$ Subscript $s$ stands for ship

[^8]:    - Crístofer H. Marques
    cristoferhood@oceanica.ufrj.br
    1 School of Engineering, Federal University of Rio Grande, Rio Grande 96203-900, Brazil
    2 Present Address: Department of Oceanic and Naval Engineering, Federal University of Rio de Janeiro, Rio de Janeiro 21945-970, Brazil

[^9]:    Crístofer Hood Marques
    cristoferhood@oceanica.ufrj.br
    1 Federal University of Rio Grande - FURG, Rio Grande, Brazil
    ${ }^{2}$ Federal University of Rio de Janeiro - COPPE/UFRJ, Rio de Janeiro, Brazil

